

A	B	C	D	E	F	
	<b>Thesis: PHI in Excel is different from PHI in mathematics</b>					1
						2
						3
	Similarity:	Standard Normal in both				4
	Difference	Density in Excel; Cumulative probability outside Excel				5
						6
	Phi(z): standard Normal <b>density</b> in Excel; <b>cumulative</b> standard Normal <b>probability</b> outside Excel					7
						8
	=PHI(z) =Norm.S.Dist(z,0)	<i>Phi inside Excel is the standard Normal density function</i>				9
		<a href="https://www.excelfunctions.net/excel-phi-function.html">https://www.excelfunctions.net/excel-phi-function.html</a>				10
		Designated by a lower-case Phi in Wikipedia				11
						12
	PHI(z) =Norm.S.Dist(z,1)	<i>Phi outside Excel is the cumulative standard Normal probability</i>				13
		<a href="https://en.wikipedia.org/wiki/Standard_normal_table">https://en.wikipedia.org/wiki/Standard_normal_table</a>				14
		Designated by upper-case (capital) Phi in Wikipedia				15
						16
	=Norm.S.Dist(z,1) - 0.5	Phi of Z>0				17
		<a href="https://mathworld.wolfram.com/NormalDistribution.html">https://mathworld.wolfram.com/NormalDistribution.html</a>				18
						19
		<b>EXCEL</b>	<b>Density</b>	<b>Density</b>	<b>Probability</b>	20
		<b>Z</b>	<b>Phi(z)</b>	<b>Norm.S.Dist(z,0)</b>	<b>=Norm.S.Dist(z,1)</b>	21
		-3	0.0044	0.0044	0.00135	22
		-2	0.0540	0.0540	0.02275	23
		-1	0.2420	0.2420	0.15866	24
		-0.5	0.3521	0.3521	0.30854	25
		0	0.3989	0.3989	0.50000	26
		0.5	0.3521	0.3521	0.69146	27
		1	0.2420	0.2420	0.84134	28
		2	0.0540	0.0540	0.97725	29
		3	<b>0.0044</b>	<b>0.0044</b>	<b>0.99865</b>	30
		=PHI(C30) =NORM.S.DIST(C30,0)			=NORM.S.DIST(C30,1)	

The PHI in these equations in the cumulative standard normal probability from minus infinity.

Mathematics

- 1  $PHI(z) = (ERF(z/\sqrt{2})+1)/2$
- 2  $ERF(z/\sqrt{2}) = 2*PHI(z)-1$
- 3  $ERF(z) = 2*PHI(z*\sqrt{2})-1$
- 4  $ERF(z/2) = 2*PHI(z/\sqrt{2})-1$

Excel

- 1  $Norm.S.Dist(z,1) = (ERF(z/\sqrt{2})+1)/2$
- 2  $ERF(z/\sqrt{2}) = 2*Norm.S.Dist(z,1)-1$
- 3  $ERF(z) = 2*Norm.S.Dist(z*\sqrt{2},1)-1$
- 4  $ERF(z/2) = 2*Norm.S.Dist(z/\sqrt{2},1)-1$

Gini (Log normal) = ERF(sigma/2) [www.statlit.org/pdf/2018-Schild-ASA.pdf](http://www.statlit.org/pdf/2018-Schild-ASA.pdf)  
[https://en.wikipedia.org/wiki/Standard\\_normal\\_table](https://en.wikipedia.org/wiki/Standard_normal_table)