| Statistical Literacy Survey |
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## Conditional Probabilities

Thesis: It is difficult to decipher (much less to write) a description or comparison of rates or percentages as presented in tables and graphs.
Survey: To ascertain the ability of collegetrained adults to decipher these statistics.

Subjects: college students (mostly working adults), professionals (mostly government data analysts) and college teachers (mostly IASE).


## Survey Subjects Comfort with Stats

"Very comfortable" dealing with formal statistics: sampling distributions, confidence intervals.

- $0 \%$ of students,
- $30 \%$ of data analysts and
- $57 \%$ of college professors.
"Very comfortable" dealing with informal statistics: rates and percentages in tables and graphs
- $7 \%$ of students,
- $62 \%$ of data analysts and
- $76 \%$ of college professors.
$\qquad$






## 100\% Row Table: Descriptions

Q23. $25 \%$ of females are blacks? [No] 44\%, 28\%, 11\%
Q25. 25\% is the percentage of blacks among females?
[No] 38\%, 28\%, 16\%.

|  | SEX |  |  |
| :---: | :---: | :---: | :---: |
| RACE | Male | Female | TOTAL |
| Black | $75 \%$ | $25 \%$ | $100 \%$ |
| White | $50 \%$ | $\mathbf{5 0} \%$ | $100 \%$ |
| Other | $40 \%$ | $60 \%$ | $100 \%$ |
| TOTAL | $50 \%$ | $50 \%$ | $100 \%$ |

## Scatter Plot: <br> the Ecological Fallacy

Q21. As the percentage of Protestants increases, the suicide rate tends to increase. [Yes] 34\%, 21\%, 32\% Q22. Protestants are more likely to commit suicide than non-Protestants (are). [No] 45\%, 49\%, 49\%.

Saying "Yes" to Q22 involves the 'ecological fallacy’: going from groups to sub-groups.


## 100\% Row Table: Comparisons

Q27. Whites are two times as likely to be female than are blacks? [No] 60\%,53\%,57\%.
Q28. Females are two times as likely to be white as to be black? [No] 44\%, 38\%, $19 \%$.
Q29. Whites are two times more likely to be female than are blacks? [No] 65\%, 49\%, 46\%.

|  | SEX |  |  |
| :---: | :---: | :---: | :---: |
| RACE | Male | Female | TOTAL |
| Black | $75 \%$ | $25 \%$ | $100 \%$ |
| White | $50 \%$ | $\mathbf{5 0} \%$ | $100 \%$ |
| Other | $40 \%$ | $60 \%$ | $100 \%$ |
| TOTAL | $50 \%$ | $50 \%$ | $100 \%$ |

## Two-Way Half Tables: <br> Descriptions

$20 \%$ of runners are female smokers? No: 55\%, 53\%, 30\% $20 \%$ of females are runners who smoke? No: 53\%, 55\%, 32\% $20 \%$ of female smokers are runners? Yes: $62 \%, 55 \%, 54 \%$ $20 \%$ of smokers are females who run? No: $42 \%, 36 \%$, $27 \%$

| PERCENTAGE WHO ARE RUNNERS |  |  |  |
| :---: | :---: | :---: | :---: |
|  | Non-smoker | Smoker | Total |
| Female | $50 \%$ | $20 \%$ | $40 \%$ |
| Male | $25 \%$ | $\mathbf{1 0} \%$ | $20 \%$ |
| Total | $37 \%$ | $15 \%$ | $30 \%$ |

## Two-Way Half Tables: Comparisons

36. The percentage of runners is twice as much among female smokers as among male smokers? Yes: $42 \%, 47 \%, 46 \%$ 37. The percentage of smokers who run is twice as much among females as among males? Yes: 41\%, 55\%, 49\%

| PERCENTAGE WHO ARE RUNNERS |  |  |  |
| :---: | :---: | :---: | :---: |
|  | Non-smoker | Smoker | Total |
| Female | $50 \%$ | $20 \%$ | $40 \%$ |
| Male | $25 \%$ | $\mathbf{1 0} \%$ | $20 \%$ |
| Total | $37 \%$ | $15 \%$ | $30 \%$ |


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| A research hospital had a higher death rate than a rural |
| hospital. Each patient's condition was classified as either |
| "poor" or "fair." |
| Q43. Is it possible that this research hospital had a lower <br> death rate than this rural hospital for those patients in <br> "poor" condition AND for those patients in "fair" <br> condition? <br> Choice of answers: Yes, No, Don't know. <br> [Yes, possible.] Error rates: 44\%, 68\%, 41\%. |

## Simpson's Paradox

A research hospital had a higher death rate than a rural hospital. Each patient's condition was classified as either "poor" or "fair."

Q43. Is it possible that this research hospital had a lower "poor" condition AND for those patients in "fair" condition?
Choice of answers: Yes, No, Don't know.
[Yes, possible.] Error rates: 44\%, 68\%, 41\%.

| Multiple Half-Tables: Description |  |  |  |
| :---: | :---: | :---: | :---: |
| Assume, "In US in 1996" ahead of each statement: <br> - $6 \%$ of low-weight births were in Calif. No: $60 \%, 43 \%, 19 \%$ <br> - $6 \%$ of Calif. births were low-weight. Yes: $39 \%, 36 \%, 11 \%$ |  |  |  |
| Percent of Births with Low Birth Weight |  |  |  |
| State | 1990 | 1995 | 1996 |
| U.S. | 7 | 7.3 | 7.4 |
| Alabama (AL) | 8.4 | 9 | 9.3 |
| California (CA) | 5.8 | 6.1 | 6 |

## Multiple Half-Tables: Comparison <br> Multiple Halt-Tables: <br> , <br> 16

Q52. In the US in 1996, there were more low-weight births in Alabama (AL) than in California (CA).
[No. No named ratio keyword] Errors: 66\%, 68\%, 30\%.

| Percent of Births with Low Birth Weight |  |  |  |
| :--- | :---: | :---: | :---: |
| State | $\mathbf{1 9 9 0}$ | $\mathbf{1 9 9 5}$ | $\mathbf{1 9 9 6}$ |
| U.S. | 7 | 7.3 | 7.4 |
|  |  |  |  |
| Alabama (AL) | 8.4 | 9 | 9.3 |
| California (CA) | 5.8 | 6.1 | 6 |

## Multiple Half-Tables: Description

Q53. 10\% of these women who received an HIV test were 40-44? No: 78\%, 55\%, 19\%.

Q54. 10\% of these women 40 to 44 had an HIV test?
Yes:
$66 \%, 68 \%$, $30 \%$.
Table 5: Percent of Women, 15 to 44,

| who Received Selected Medical Services |  |  |  |
| :---: | :---: | :---: | :---: |
| Age | HV | Pregnancy | Pap |
| $15-19$ | 14.6 | 16.1 | 33.5 |
| $20-24$ | 20 | 27.4 | 68.7 |
| $25-29$ | 25.6 | 25.3 | 70.9 |
| $30-34$ | 18.5 | 17.4 | 69.5 |
| $35-39$ | 14.2 | 8.1 | 62.9 |
| $40-44$ | 10 | 4.3 | 62.7 |
| ALL | 17.3 | 16 | 61.9 |

## Multiple Half-Tables: Description

Assume, "In 1990" ahead of each statement:
Q45. $26.2 \%$ of blacks were smokers. Yes: $60 \%, 43 \%, 19 \%$ Q46. 26.2\% of smokers were black. No: 72\%, $62 \%$, 32\%.
Table 3: Percentage of Smoking Prevalence

| Year | All | Male | Female | White | Black |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1955 | -- | 56.9 | 28.4 |  | -- | -- |
| 1965 | 42.4 | 51.9 | 33.9 |  | 42.1 | 45.8 |
| 1980 | 33.2 | 37.6 | 29.3 |  | 32.9 | 36.9 |
| 1990 | 25.5 | 28.4 | 22.8 | 25.6 | 26.2 |  |

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| Year | All | Male | Female | White | Black |
| :---: | :---: | :---: | :---: | :---: | :---: |





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    Survey Evaluation
Possible answers: Strongly agree, Moderately agree,
    Moderately disagree and Strongly disagree.
Q64. This survey was much more difficult than I thought it
    would be. 25%,50%, 20%,5%
Q66. This survey was unnecessarily tricky.
    24%, 27%, 36%, 14%
Q68. These tables and graphs are the kind I need or want
    to be able to read or understand. 53%, 37%,7%,4%.
Q69. College students should be able to read these kinds of
    tables and graphs. 63%,29%,5%,2%.
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## StatLit Survey Error Rate

The average error rate was about

- $50 \%$ for college students,
- $45 \%$ for data analysts and
- 30\% for college teachers.

Using data analysts’ 80th percentile score (67\% correct), the following reached that level:

- $5 \%$ of students,
- $20 \%$ of data analysts
- $45 \%$ of college teachers


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\begin{aligned}
& \text { Conclusion } \\
& \text { Describing and comparing rates \& percentages is } \\
& \text { conditional probability in ordinary English. } \\
& \text { Statistical educators will be seen as negligent } \\
& \text { if most of their students cannot read - much less } \\
& \text { write - descriptions \& comparisons of rates \& } \\
& \text { percentages as presented in tables and graphs. } \\
& \text { Statistical educators should accept responsibility for } \\
& \text { teaching students how to read and write ordinary } \\
& \text { English descriptions and comparisons of rates and } \\
& \text { percentages as found in tables and graphs. }
\end{aligned}
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Try teaching this in your intro stats class.


## Related Articles at

## www.StatLit.org

Schield, Milo (2004). Statistical Literacy and Liberal Education at Augsburg College. AAC\&U Peer Review. See www.StatLit.org/pdf/2004SchieldAACU.pdf.
Schield, Milo (2000). Difficulties in Describing and Comparing Rates and Percentages. 2000 ASA Section on Statistical Education. P. 176. See www.StatLit.org/pdf/2000SchieldASA.pdf.

Schield, Milo (2001). Statistical Literacy: Reading Tables of Rates and Percentage. ASA Proceedings of Statistical Education Section. See www.StatLit.org/pdf/2001SchieldASA.pdf
Schield, Milo (2004). Statistical Literacy Curriculum Design. IASE. See www.StatLit.org/pdf/2004SchieldIASE.pdf.

