












## Big Data and Big Ideas

Big data: "any data set in which all associations are statistically significant." [Schield definition] Leaving aside local experiments (A-B tests), it might seem that intro statistics - statistical significance - has little value with 'big data'. In big data,

1. Coincidence is a bigger problem,
2. Confounding is often the \#1 problem.

The "Birthday" Problem: Chance of same birthday


Source: www.statlit.org/Excel/2012Schield-Bday.xls.


| Connections and Chance |  |  |
| :---: | :---: | :---: |
| Pairs | GROUP | Details |
| 196 | Quadrants 1-4 | 49 pairs each |
| 49 | Left-to-Right |  |
| 49 | Top-to-Bottom |  |
| 84 | Within each side | 21 pairs each |
| 378 | TOTAL |  |
| A preselected birthday match has one chance in 365 . In a group of 28 , we have 378 pairs: $(\mathrm{N}-1)(\mathrm{N} / 2)$. A somewhere match is expected -> $50 \%$ of the time. |  |  |



## Coincidence: Flipping a fair coin Getting a "run" of heads

Conjecture:
The longer
the run,
the more unlikely the outcome.

Empirical test



Run of 4 heads: 1 chance in $\mathbf{2 N}^{\wedge} \mathbf{4}=1 / 16$
Run of 19 heads: 1 in $2^{\wedge} 19=1 / 524,288$


## Consider a run of 10 heads? What is the chance of that?

Question is ambiguous! Doesn't state context!

1. Chance of 10 heads on the next $\mathbf{1 0}$ flips?
$\mathrm{p}=1 / 2 ; \mathrm{k}=10$.
$\mathrm{P}=\mathrm{p}^{\wedge} \mathrm{k}=(1 / 2)^{\wedge} 10=$ one chance in 1,024
2. Chance of at least one run of 10 heads
somewhere when flipping 1,024 sets* of 10 coins each? At least 50\%

* or (conjecture) when flipping 1,033 coins: $1 / \mathrm{p}+\mathrm{k}-1$.

Law of Very-Large Numbers (Qualitative):
The unlikely is almost certain given enough tries

Law of Expected Values:
Consider N tries with events having one chance in N .

* One event 'expected' in N tries
* Chance of at least one $>50 \%$



## Second Big Idea: Confounding

Big data will force statistical education to deal with causation in observational studies.

1. Most big data are observational.
2. Most big data users want to use associations as evidence for causation.
3. Confounding is the \#1 problem.
4. 'Confound', 'predict' and explain', will need clarification.

## Confounding: Two definitions

Confounder (math): Associated/observational
Any factor associated with the predictor (independent) and with the outcome (dependent) in an association.

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Any factor associated with the predictor (independent) and with the outcome (dependent) in an association:

- that is not caused by the predictor, and
- that has a causal influence on the outcome.


## Prediction: Two definitions

Prediction (math): Associated/observational
Modelled result assuming none of the factor levels are set by a researcher.

Prediction (Business): Causal/Experimental
Modelled results based on factor levels
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## Explain: Two definitions

Explain (math): Associated/observational
How much of the outcome variation is associated with or attributable to a given factor.*

Explains (Business): Causal/Experimental
How much of the outcome variation is a result of or caused by a factor.*

* 'Due to' and 'because of' are "in-between"

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## Ambiguity in "Explains"

For every $5 \#$ increase in weight in adult men, height increases by 1 inch.
Does the five pound increase in weight "explain" the one inch increase in height?

- Yes, if explain means "is associated with": we shift focus from light-weight men to heavy-weight men at a given time.
- No, if explains means "causes": we increase the weight of individual men over time.

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| Modeling: |
| :--- |
| What to Take into Account |
| Consider modeling the outcome in this causal diagram: |
| Predictor $\rightarrow$ Confounder $\rightarrow$ Outcome |
| Kaplan: Model Outcome on Predictor |
| Schield: Model Outcome on Predictor and Confounder |
| 1.Who is right? |
| 2. Can both be right? YES!!! |
| Schield in predicting; Kaplan in causal explaining. |

## Modeling:

What to Take into Account
Consider modeling the outcome in this causal diagram:
Predictor $\rightarrow$ Confounder $\rightarrow$ Outcome
Kaplan: Model Outcome on Predictor
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1.Who is right?
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## 26 <br> Causation \& Simpson's Paradox

Simpson's paradox is not a paradox in prediction. Simpson's paradox is only a paradox in forming a causal explanation or conclusion.

In a prediction the signs and sizes of the coefficients are all but irrelevant. R-sq is what counts.
In a causal explanation, the size and sign of the coefficients matter. R-sq is all but irrelevant.

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## Conclusion

Many - if not most - big-data users want causal explanations and causal predictions.

Math-stats can help us explain why coincidence increases as the size of the data increases.

Mathematics doesn't study causation. There is no mathematical operator or operation for causes.

Statistics education must say more about causation than simply saying "Association is not Causation."

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## Recommendations

1. Schield (2011) Coincidence in Runs and Clusters www.statlit.org/pdf/2012Schield-MAA.pdf
2. Pearl (2000). Simpson's Paradox: An Anatomy. http://bayes.cs.ucla.edu/R264.pdf
3. Pearl (2009), Causal inference in statistics. http://ftp.cs.ucla.edu/pub/stat_ser/r350.pdf
4. Gelman blog (2014). On Simpson's Paradox. http://andrewgelman.com/2014/02/09/keli-liu-xiao-li-meng-simpsons-paradox/

# TWO BIG IDEAS IN TEACHING BIG DATA 

# Coincidence \& Confounding 

by<br>Milo Schield<br>Twin-Cities Chapter Meeting March 19, 2014. Augsburg College www.StatLit.org/pdf/2014-Schield-ASA-TCC-6up.pdf

## Big Data and Big Ideas

Big data: "any data set in which all associations are statistically significant." [Schield definition]
Leaving aside local experiments (A-B tests), it might seem that intro statistics - statistical significance - has little value with 'big data'.
In big data,

1. Coincidence is a bigger problem,
2. Confounding is often the \#1 problem.

## Coincidence?



## The "Birthday" Problem: Chance of same birthday



Richard von Mises (1883-1953)
In a group of 28 people,
a birthday match (same month and day) is expected.'


## The "Birthday" Problem Math Answer

$\mathrm{N}!/[\mathrm{k}!(\mathrm{N}-\mathrm{k})!]$ combos of N things taken k at a time.
For $\mathrm{k}=2$, \#combos $=\mathrm{C}=\mathrm{N}(\mathrm{N}-1) / 2 \sim\left(\mathrm{~N}^{\wedge} 2\right) / 2$
$\mathrm{N} \sim \operatorname{sqrt}(2 \mathrm{C})$. If $\mathrm{C}=365, \mathrm{~N} \sim \operatorname{Sqrt}(730)=27$.
Q. Are students convinced? No!!!

If the chance of an event is $p$ and $p=1 / n$, then this event is "expected" in $n$ trials.
Show students there are > 365 pairs w 28 people.

## Consider a table

Table with 28 people -- seven on each of four sides.

|  | © | $\stackrel{+}{ }$ | (2) | ${ }^{\text {© }}$ | $\stackrel{+}{ }$ | (2) | © |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| (-) |  |  |  |  |  |  |  | ${ }^{(6)}$ |
| $\stackrel{\square}{+}$ |  |  |  |  |  |  |  | $\odot$ |
| (2) |  |  |  |  |  |  |  | (2) |
| © |  |  |  |  |  |  |  | (-) |
| $\odot$ |  |  |  |  |  |  |  | $\stackrel{+}{ }$ |
| * |  |  |  |  |  |  |  | (2) |
| (-) |  |  |  |  |  |  |  | (-) |
|  | (3) | ¢ | (2) | () | 앙 | (2) |  |  |

Source: www.statlit.org/Excel/2012Schield-Bday.xls.

## Get Birthdays (Mn/Dy): Color cell with row-column match

| Schield (2012) |  |  | RICHARD VON MISES' BIRTHDAY PROBLEM |  |  |  |  |  |  |  |  | V2b |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | Press F9 for a new group of 28 people |  |  |  |  |  |  |  |  |  |
|  |  | Month | 9 | 10 | 9 | 4 | 7 | 4 | 11 |  |  |  |
|  |  | Day | 24 | 3 | 26 | 26 | 18 | 28 | 6 |  |  |  |
| Month | Day |  | ¢) | $\Theta$ | (8) | $\odot$ | $\Theta$ | (8) | (\%) |  | Month | Day |
| 4 | 9 | (9) |  |  |  |  |  |  |  | (9) | 2 | 15 |
| 8 | 10 | 9 |  |  |  |  |  |  |  | (9) | 7 | 18 |
| 2 | 20 | (8) |  |  |  |  |  |  |  | (8) | 5 | 19 |
| 6 | 30 | (9) |  |  |  |  |  |  |  | (9) | 8 | 15 |
| 2 | 22 | $\odot$ |  |  |  |  |  |  |  | $\Theta$ | 5 | 9 |
| 6 | 17 | () |  |  |  |  |  |  |  | (9) | 7 | 25 |
| 1 | 15 | (9) |  |  |  |  |  |  |  | (9) | 4 | 11 |
|  |  |  | $\bigcirc$ | (9) | (8) | ¢ | $\Theta$ | (8) | (\%) |  |  |  |
|  |  | Month | 4 | 1 | 6 | 12 | 11 | 6 | 3 |  |  |  |
|  |  | Day | 7 | 27 | 26 | 4 | 11 | 18 | 9 |  |  |  |

## Four Quadrants: 49 possible connections each

Schield (2011) RICHARD VON MISES' BIRTHDAY PROBLEM 28 People

|  |  | Month | 10 | 11 | 11 | 9 | 4 | 7 | 6 |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Day | 16 | 18 | 8 | 9 | 13 | 25 | 24 |  |  |
| Month | Day |  |  |  |  |  |  |  |  | Month | Day |
| 8 | 20 |  |  |  |  |  |  | 1 |  | 7 | 25 |
| 10 | 29 |  |  |  |  |  |  |  |  | 8 | 16 |
| 4 | 11 |  |  |  |  |  |  |  |  | 11 | 6 |
| 3 | 3 |  |  |  |  |  |  |  |  | 11 | 29 |
| 1 | 3 |  |  |  |  |  |  |  |  | 8 | 3 |
| 3 | 30 |  |  |  |  |  |  |  |  | 3 | 24 |
| 10 | 28 |  |  |  |  |  |  |  |  | 1 | 15 |
|  |  |  |  |  |  |  |  |  |  |  |  |
|  |  | Month | 5 | 2 | 6 | 2 | 1 | 7 | 5 |  |  |
|  |  | Day | 28 | 8 | 6 | 12 | 14 | 1 | 25 |  |  |

Source: www.statlit.org/Excel/2012Schield-Bday.xls.

## Top-to-Bottom \& Left-to-Right: 49 connections each

Schield (2011) RICHARD VON MISES' BIRTHDAY PROBLEM 28 People

|  |  | Month | 11 | 8 | 10 | 10 | 8 | 10 | 3 |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Day | 19 | 3 | 28 | 17 | 27 | 29 | 5 |  |  |
| Month | Day |  |  |  |  | S |  |  |  | Month | Day |
| 5 | 23 |  |  |  |  |  |  |  |  | 1 | 12 |
| 1 | 1 |  |  |  |  |  |  |  |  | 11 | 17 |
| 9 | 6 |  |  |  |  |  |  |  |  | 12 | 3 |
| 10 | 13 |  |  |  |  |  |  |  |  | 7 | 29 |
| 7 | 14 |  |  |  |  |  |  |  |  | 2 | 17 |
| 8 | 30 |  |  |  |  |  |  |  |  | 4 | 2 |
| 1 | 8 |  |  |  |  |  |  |  |  | 8 | 17 |
|  |  |  |  |  | N |  |  |  |  |  |  |
|  |  | Month | 12 | 3 | 10 | 9 | 12 | 9 | 5 |  |  |
|  |  | Day | 24 | 6 | 17 | 19 | 1 | 20 | 29 |  |  |

## Same-Edge (four): 21 connections each

Schield (2011) RICHARD VON MISES' BIRTHDAY PROBLEM 28 People

|  |  | Month | 3 | 2 | 2 | 3 | 9 | 3 | 5 |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Day | 4 | 5 | 9 | 29 | 20 | 5 | 20 |  |  |  |
| Month | Day |  |  |  |  |  |  |  |  |  | Month | Day |
| 6 | 22 |  |  |  |  |  |  |  |  | E | 4 | 1 |
| 10 | 8 |  |  |  |  |  |  |  |  |  | 7 | 10 |
| 5 | 5 |  |  |  |  |  |  |  |  |  | 3 | 26 |
| 11 | 23 |  |  |  |  |  |  |  |  |  | 3 | 10 |
| 3 | 27 |  |  |  |  |  |  |  |  | E | 4 | 1 |
| 10 | 2 |  |  |  |  |  |  |  |  |  | 9 | 8 |
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## Connections and Chance

| Pairs | GROUP | Details |
| :---: | :--- | :--- |
| 196 | Quadrants 1-4 | 49 pairs each |
| 49 | Left-to-Right |  |
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A preselected birthday match has one chance in 365.
In a group of 28 , we have 378 pairs: ( $\mathrm{N}-1$ )( $\mathrm{N} / 2$ ).
A somewhere match is expected $->50 \%$ of the time.

## Coincidence: Flipping a fair coin Getting a "run" of heads

Conjecture:
The longer
the run,
the more unlikely
the outcome.

Empirical test


## Flip coins in rows. 1=Heads Red = Run of heads.



## Run of 4 heads: 1 chance in 2^4 = 1/16 Run of 19 heads: 1 in 2^19 = 1/524,288



Source: www.statlit.org/Excel/2012Schield-Runs.xls

## Consider a run of 10 heads? What is the chance of that?

Question is ambiguous! Doesn't state context!

1. Chance of 10 heads on the next $\mathbf{1 0}$ flips?

$$
\begin{aligned}
& \mathrm{p}=1 / 2 ; \mathrm{k}=10 . \\
& \mathrm{P}=\mathrm{p}^{\wedge} \mathrm{k}=(1 / 2)^{\wedge} 10=\text { one chance in } 1,024
\end{aligned}
$$

2. Chance of at least one run of 10 heads somewhere when flipping 1,024 sets* of 10 coins each? At least 50\%

* or (conjecture) when flipping 1,033 coins: $1 / \mathrm{p}+\mathrm{k}-1$.


## Coincidence increases as data size increases



## Law of Coincidence

Law of Very-Large Numbers (Qualitative):
The unlikely is almost certain given enough tries

Law of Expected Values:
Consider N tries with events having one chance in N .

* One event 'expected' in N tries
* Chance of at least one > $50 \%$



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2. Most big data users want to use associations as evidence for causation.
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## Explain: Two definitions

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## Common Confusions

Among adult men:

1. Weight and height are positively correlated.
2. Those who are heavier are generally taller than those who are thinner.
3. As weight increases, height increases.
4. For every extra $5 \#$, height increases by 1 inch
5. If you gain weight, you will grow taller.

## Ambiguity in "Explains"

For every $5 \#$ increase in weight in adult men, height increases by 1 inch.
Does the five pound increase in weight "explain" the one inch increase in height?

- Yes, if explain means "is associated with": we shift focus from light-weight men to heavy-weight men at a given time.
- No, if explains means "causes": we increase the weight of individual men over time.


## Multivariate Analysis Predict vs. "Explain"

| Step | 1 | 2 | 3 |
| :--- | :---: | :---: | :---: |
| Constant | $\$ 80,000$ | $\$ 78,000$ | $\$ 58,000$ |
|  |  |  |  |
| Baths | $\$ 39,000$ | $\$ 36,000$ | $\$ 15,000$ |
| per bath |  |  |  |
| Acres |  | $\$ 7,500$ | $\$ 7,500$ |
| per acre |  |  |  |
| Area |  |  | $\$ 33$ |
| p-sq | $44 \%$ | $60 \%$ | $68 \%$ |

Predict/observe: accuracy $\uparrow$ as factors $\uparrow$ \#3: Each extra bath explains a $\$ 15 \mathrm{~K} \uparrow$ in value.
Predict/causal: If a bathroom is added, the house value is expected to $\uparrow$ by $\$ 15 \mathrm{~K}$.

## Modeling: What to Talke into Account

Consider modeling the outcome in this causal diagram:
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Kaplan: Model Outcome on Predictor
Schield: Model Outcome on Predictor and Confounder
1.Who is right?
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Schield in predicting; Kaplan in causal explaining.

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In a causal explanation, the size and sign of the coefficients matter. R-sq is all but irrelevant.

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