| StatLit Slkills Survey |
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| MILO SCHIELD, <br> Augsburg College <br> Director, W. M. Keck Statistical Literacy Project <br> Vice President, National Numeracy Network <br> Project Kaleidoscope (PKAL) <br> Carleton College: QUIRK Project <br> Quantitative Inquiry, Reasoning \& Knowledge <br> 11 October 2008 <br> Slides at www.StatLit.org/pdf/2008SchieldPKAL6up.pdf |




## Hard questions:

Which compare fits this table?

| a. $9 \%$ <br> a. <br> b. $25 \%$ <br> c. $53 \%$ | Adults | SEX |  |  |
| :--- | :---: | :---: | :---: | :---: |
|  | Black | Men | Women | ALL |
|  | White | $51 \%$ | $25 \%$ | $100 \%$ |
|  | Other | $40 \%$ | $60 \%$ | $100 \%$ |
|  | ALL | $52 \%$ | $48 \%$ | $100 \%$ |

a. Women are more likely among whites than blacks.
b. Blacks are more likely among men than women.
c. Either of the above d. None of above e. Don't know.
' $a$ ' is correct. $91 \%$ missed this. $\quad[R=0.21]$

## Hard Questions: Compare: 'Times more than'

Eight is three times more than two.
a. True b. False c. Don't know

| $14 \%$ | $82 \%$ | $4 \%$ |
| :--- | :--- | :--- |

Answer: A. True
Analysis: This statement means literally,
a) ' 8 is 3 times (two) more than 2 ' $8=6+2$
$86 \%$ missed this. $\quad[\mathrm{R}=0.00]$

## nocroses penc cauk <br> Hard Questions: Confusion of the Inverse

A medical test for HIV has 95\% accuracy:
$>95 \%$ of those with HIV test positive.
Suppose that most of the subjects are like you.
No risky sex practices; no intravenous drugs.
You test positive. What is your chance of having HIV? What percentage of these positives have HIV?
a. Less than $95 \%$
b. $95 \%$
c. More than $95 \%$
d. Don't know or Not sure

Answer: A 84\% missed this $(\mathrm{R}=0.05)$



## 110 cl 2008 pral Luink <br> Good Question: <br> Understand Assembly [R=0.44]

Which definition of 'heat-wave deaths' gives the largest number?
a. deaths caused by a heat wave
b. deaths occurring during a heat-wave
c. No difference
d. d. Don't know/not sure

Answer: B. $\quad 51 \%$ missed this.
$28 \%$ choose A, 49\% B, 17\% C and 6\% D

## 110 C 2008 p Kall Quir <br> Good Question: \%\% vs. \$\$ Change [R=0.35]

If incomes of rich and poor both increase at the same rate, the income gap between rich and poor will
a. decrease
b. stay the same
c. increase
d. Don't know.

Answer: C. 81\% missed this.
How: $\$ 90 \mathrm{~K}$ versus $\$ 30 \mathrm{~K}$ is a $\$ 60 \mathrm{~K}$ difference. Doubling both incomes doubles the difference.
Percentage change (multiplicative) is not additive
Modeling Error

| \# Questions | $\mathbf{1 0}$ Q | $\mathbf{1 5} \mathbf{Q}$ | $\mathbf{2 0}$ Q | $\mathbf{2 5} \mathbf{Q}$ | $\mathbf{3 0} \mathbf{Q}$ | $\mathbf{3 5} \mathbf{Q}$ | $\mathbf{6 9}$ Q |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Correlation | 0.82 | 0.88 | 0.90 | 0.90 | 0.94 | 0.94 |  |
| Min | $0 \%$ | $7 \%$ | $15 \%$ | $16 \%$ | $20 \%$ | $20 \%$ | $26 \%$ |
| Max | $90 \%$ | $87 \%$ | $85 \%$ | $84 \%$ | $83 \%$ | $83 \%$ | $75 \%$ |
| Average | $58 \%$ | $60 \%$ | $55 \%$ | $52 \%$ | $52 \%$ | $53 \%$ | $52 \%$ |
| StdDev | $17 \%$ | $15 \%$ | $14 \%$ | $14 \%$ | $12 \%$ | $12 \%$ | $10 \%$ |
| R-sq | 0.82 | 0.91 | 0.94 | 0.96 | 0.97 | 0.98 |  |
| Adj. R-sq | 0.81 | 0.89 | 0.93 | 0.95 | 0.96 | 0.97 |  |

## Sampling Error

Suppose a student scores $50 \%$ on a true-false test. What is the margin of error due to sampling?

For a 100 question test, the $95 \%$ margin of error is $10 \%$. The true score is between $40 \%$ and $60 \%$.

For a 25 question test, the $95 \%$ margin of error is $20 \%$. The true score is between $30 \%$ and $70 \%$.

Sampling error is separate from modeling error.

## Content Validity

Even if an instrument had no modeling error and no sampling error, it might lack content validity.

Content validity is the extent to which experts believe a measure represents a social concept -- such as depression, intelligence or statistical literacy.

| Next Step |
| :--- |
| The content validity of any measure of numeracy, |
| quantitative literacy or statistical literacy |
| must be appraised by subject matter experts. |
| Once an instrument is found to have content |
| validity and reliability then trade offs |
| between number of questions and error |
| (model and sampling) can be addressed. |
| At that point, a short reliable survey to |
| assess statistical literacy can be designed. |


| Statistical Literacy Assessment References |
| :---: |
| Schield, Milo (2008). Statistical Literacy Skills Survey. PKAL-QuIRK conference at Carleton College. See www.StatLit.org/pdf/2008SchieldPKAL.pdf |
| Schield, Milo (2008). Statistical Literacy: Assessing <br> Case Studies. Draft of paper submitted to ViSA: <br> Variety in Statistics Assessment (UK). <br> See www.StatLit.org/pdf/2008SchieldViSA.pdf. |

