## Chapter 3: Overview

# Statistical Literacy 2009 Chapter Summaries <br> by <br> Milo Schield 

www.StatLit.org/pdf/...
2009StatLitTextHandoutCh3.ppt
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## Ch 1. Review

## Statistics are generally

 used as evidence to support an argument.The influences on a statistic are of four kinds: Context, Assembly, Randomness or Error.

The Point or the Target

The more disputable the point, the stronger the evidence must be.

Statistic As Evidence
"All Statistics are Socially Constructed"
So, "Take CARE"!!
Statistics may be influenced by:

| C | A | R | E |
| :---: | :---: | :---: | :---: |
| Confounding | Assembly | Randomness | Error |

## Review of C.A.R.E.

Context: Related factors taken into account; the confounders not taken into account.

Assembly: Choice in definition, measurement or presentation.

Randomness: Influence of chance.
Error: Systematic deviation of statistics from the underlying reality.

## Describe Distributions: Percentiles

Table 7 Distribution of Heights for U.S. Twenty-year olds

| Percentile | $3^{\text {rd }}$ | $5^{\text {th }}$ | $10^{\text {th }}$ | $25^{\text {th }}$ | $50^{\text {th }}$ | $75^{\text {th }}$ | $90^{\text {th }}$ | $95^{\text {th }}$ | $97^{\text {th }}$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Male | 64.3 | 65.0 | 66.0 | 67.7 | 69.6 | 71.5 | 73.2 | 74.2 | 74.9 |
| Female | 59.5 | 60.1 | 61.0 | 62.6 | 64.3 | 66.0 | 67.6 | 68.5 | 69.1 |

Table 8 Distribution of Weights for U.S. Twenty-year olds

| Percentile | $3^{\text {td }}$ | $5^{\text {th }}$ | $10^{\text {th }}$ | $25^{\text {th }}$ | $50^{t^{\text {th }}}$ | $75^{\text {th }}$ | $90^{\text {th }}$ | $95^{\text {th }}$ | $97^{\text {th }}$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Boys | 119 | 123 | 129 | 140 | 156 | 175 | 196 | 211 | 222 |
| Girls | 99 | 102 | 107 | 116 | 128 | 145 | 166 | 183 | 196 |

## Describe Distributions: Mean, Median \& Mode



## Describe Distributions: Comparisons

2000 U.S. Family Incomes by Number of Wage Earners

| $\#$ <br> Earners | Median <br> Income | Mean <br> Income | Income per <br> family member |
| :--- | :---: | :---: | :---: |
| None | 21,916 | 27,720 | 12,054 |
| 1 | 34,423 | 50,188 | 16,779 |
| 2 or more | 67,600 | 82,267 | 23,762 |
| 2 | 63,816 | 79,113 | 24,965 |
| 3 | 76,566 | 90,330 | 21,270 |
| 4 or more | 91,709 | 103,678 | 19,375 |
| ALL | 50,890 | 65,574 | 20,865 |

## Compare Distributions: Trends



## Standardizing Totals: "talking into account"

State Prison Operating Expenses: CA vs. NY

| State | Total | \# Inmates | Per Inmate |
| :--- | :---: | :---: | :---: |
| CA | $\$ 2.9 \mathrm{~B}$ | 136 K | $\$ 21,385$ |
| NY | $\$ 1.9 \mathrm{~B}$ | 69 K | $\$ 28,426$ |


| Total | Per Inmate |
| :---: | :---: |
| $50 \%$ more | $25 \%$ less |
| than | than |

Controlling for prison population reverses the association.
State Prison Operating Expenses: MD vs. KS

| State | Total | \# Inmates | Per Inmate |
| :--- | :---: | :---: | :---: |
| MD | $\$ 481 \mathrm{M}$ | 21,623 | $\$ 22,245$ |
| KS | $\$ 159 \mathrm{M}$ | 7,148 | $\$ 22,245$ |$\quad$| Total | Per Inmate |
| :---: | :---: | :---: |
| 3 times | Same |
| as much as | as |

Controlling for prison population nullifies the association.

## Standardizing Totals: "talking into account"

State Prison Operating Expenses: MN vs. ME

| State | Total | \# Inmates | Per Inmate |
| :--- | :---: | :---: | :---: |
| MN | $\$ 184 \mathrm{M}$ | 4,865 | $\$ 37,825$ |
| ME | $\$ 48 \mathrm{M}$ | 1,424 | $\$ 33,711$ |


| Total | Per Inmate |
| :---: | :---: |
| $260 \%$ more | $12 \%$ more |
| than | than |

Controlling for prison population decreases the association.
State Prison Operating Expenses: MN vs. IA

| State | Total | \# Inmates | Per Inmate |
| :---: | :---: | :---: | :---: |
| MN | $\$ 184 \mathrm{M}$ | 4,865 | $\$ 37,825$ |
| IA | $\$ 144 \mathrm{M}$ | 5,929 | $\$ 24,286$ |


| Total | Per Inmate |
| :---: | :---: |
| $27 \%$ more | $56 \%$ more |
| than | than |

Controlling for prison population increases the association.

## Standardizing Averages: "talking into account"

NAEP 2000 8 $^{\text {th }}$ Grade Math Scores: VA vs. TX

|  | Encyclopedia at home |  |  |
| :--- | ---: | :---: | :---: |
| State | All | Yes | No |
| Virginia (VA) | $275(100 \%)$ | $278(81 \%)$ | $241(19 \%)$ |
| Texas (TX) | $\uparrow 273(100 \%)$ | $\downarrow 279(73 \%)$ | $\downarrow 242(27 \%)$ |

Virginia students did better than Texas students.
After taking into account encyclopedias at home, Texas students did better than Virginia students.

## Standardizing Averages: "talking into account"

SAT Verbal Scores by Race: 2002 vs. 1981

| GROUP | $\mathbf{1 9 8 1}$ | $\mathbf{2 0 0 2}$ | CHANGE |
| :--- | :---: | :---: | :---: |
| White | $519(85 \%)$ | $527(65 \%)$ | +8 |
| Black | $412(9 \%)$ | $431(11 \%)$ | +19 |
| Asian | $474(3 \%)$ | $501(10 \%)$ | +27 |
| Mexican | $438(2 \%)$ | $446(4 \%)$ | +8 |
| Puerto Rican | $437(1 \%)$ | $455(3 \%)$ | +18 |
| American Indian | $471(0 \%)$ | $479(1 \%)$ | +8 |
| ALL Test takers | $\mathbf{5 0 4}$ | $\mathbf{5 0 4}$ | ZERO |

SAT scores were the same in 2002 as in 1981.
After taking into account race, SAT scores were higher in 2002 than in 1981.

## Single Weighted Average



## Comparing Weighted Averages



## Standardizing: "Same mix"



| Race | Married | Single |
| :--- | :---: | :---: |
| White <br> $(100 \%)$ | $\$ 60,600$ <br> $(82 \%)$ | $\$ 26,700$ <br> $(18 \%)$ |
| Black | $\$ 53,900$ <br> $(100 \%)$ | $\$ 14,000$ <br> $(48 \%)$ |
| $(52 \%)$ |  |  |

## Family Income: Plotting the data

Mean Family Income by Race \& Structure


No Percentage who are headed by Married Couple Yes

| Race | Married | Single |
| :--- | :---: | :---: |
| White <br> $(100 \%)$ | $\$ 60,600$ <br> $(82 \%)$ | $\$ 26,700$ <br> $(18 \%)$ |
| Black <br> $(100 \%)$ | $\$ 53,900$ <br> $(48 \%)$ | $\$ 14,000$ <br> $(52 \%)$ |

## Calculate Averages

Mean Family Income by Race \& Structure


## Standardizing

$78 \%$ of all US families are headed by a married couple


## Comparisons: Black-White Income Gap

| Average Income | Before | After |
| :--- | :---: | :---: |
| Whites | 55 K | 53 K |
| Blacks | 33 K | 45 K |
| Difference | 22 K | 8 K |

Of the $\$ 22 \mathrm{~K}$ black-white income gap, $14 \mathrm{~K}(22-8)$ is explained by family structure.
$67 \%(14 / 22)$ of the black-white income gap is explained by marital status.

## Three methods

If you're having difficulty using the graphical approach, you can use either proportional reasoning or the algebra of weighted averages. As you've seen, they give the same result as the graphical approach. A common error in using either is to multiply by the percentages. The proper approach is to convert the percentages to decimals before multiplying.
Here are problems associated with each of these three methods.

- Graphically: a common problem is identifying what numbers one places on the right and the left sides of the graph.
- Proportional reasoning: a common problem is identifying whether to add onto the smaller or subtract from the larger.
- Algebra: a common problem is deciding which percentage to apply to which value.


## Sumninary

Context involves what is (not) taken into account.
What is taken into account can influence

- Counts or totals (by forming ratios)
- Averages (by selection or standardizing)

Hypothetical thinking is required to think of what could have been taken into account (confounders).
"Presenting Confounding and Standardization Graphically" STATS Magazine at www.StatLit.org/pdf/2006SchieldSTATS.pdf

