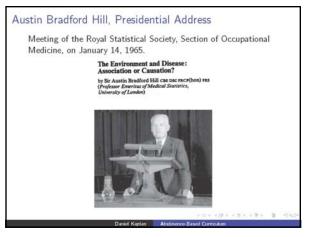
Daniel Kaplan Macalester College St. Paul, Minnesota, USA November 10, 2010

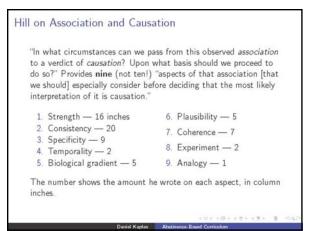
Abstract:

The subtitle might have been, "How religious fervor has shaped the way we teach statistics." But this would mislead you into thinking about actual religion and contemporary disputes about evolution, sex education, and so on.

No, the talk will be about plain, old, everyday introductory statistics and the familiar topics that are studied: the t-test, one-and two-tailed tests, association vs. causation, etc.

The conventional choice of topics and approaches, it will be claimed, is based largely on honoring the faith of our statistical fathers and the quasi-theological disputes of old, and not on extracting useful information from the sorts of data commonly encountered today. With an eye toward curricular reformation, a few theses will be offered.





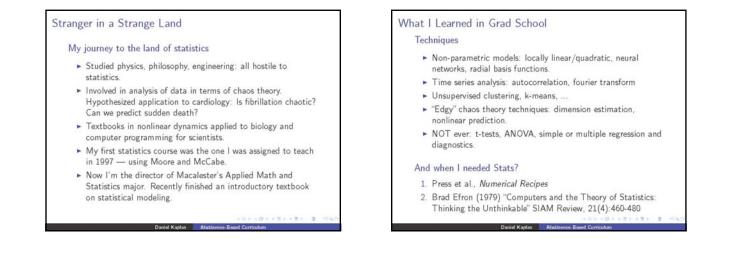


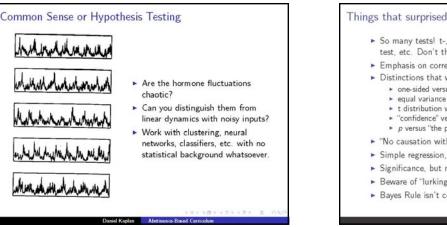
"Occasionally, it is possible to appeal to experimental, or semi-experimental, evidence. For example, because of an observed association some preventive action is taken. Does it in fact prevent? The dust in the workshop is reduced, lubricating oils are changed, persons stop smoking cigarettes. Is the frequency of the associated events affected? Here the strongest support for the causation hypothesis may be revealed." Hill on Tests of Significance

"... the glitter of the *t* table diverts attention from the inadequacies of the fare. Only a tithe, and an unknown tithe, of the factory personnel volunteer for some procedure or interview, 20% of patients treated in some particular way are lost to sight, 30% of a randomly-drawn sample are never contacted. The sample may, indeed, be akin to that of the man who, according to Swift, 'had a mind to sell his house and carried a piece of brick in his pocket, which he showed as a pattern to encourage purchasers.' "

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Things that surprised me when I started teaching stats ► So many tests! t-, p-, z-, paired-t, chi-squared test, rank-sum test, etc. Don't they have a common underlying logic? Emphasis on correlation coefficient, t, not effect size.

- Distinctions that were too subtle for students.
 - one-sided versus two-sided (or is it "tailed"?)
 - equal variance versus unequal variance t-test + t distribution with 10 or 20 d.f. versus normal.
 - "confidence" versus "probability"
 - p versus "the probability of the null is true"
- "No causation without experimentation."
- Simple regression, but not multiple regression.
- Significance, but not power.
- Beware of "lurking variables"!
- ► Bayes Rule isn't central! Support for decisions not central!

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To an outsider, some problems are obvious

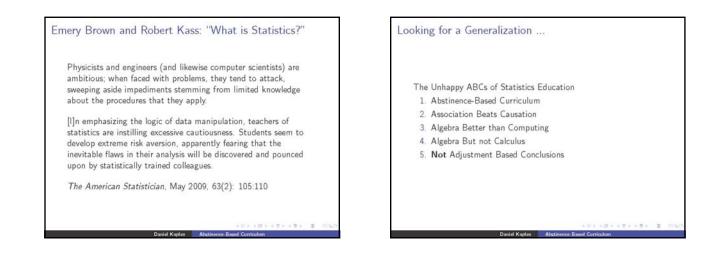
- There's no big picture!
 - Archaic and misleading language: e.g., "significance", "deviation," "error," "standard"
 - Don't teach algorithms, but how to use the algorithms.
 - Need measures of effect size, not just correlation. Units are important in science!
 - To be interesting, statistics has to deal with situations of interesting complexity. Can't be about means versus medians.
 - There's lots of judgment in statistics, to give students settings that require judgment, e.g., Which model is best? What's a normal value in this setting?
 - Students don't understand even simple formulas, e.g. s/\sqrt{n}
 - Archaic technology, e.g. tables, and failure to adopt computing
 - Adopting computing means teaching about computing, because nobody else is doing it.
 - Using teaching software instead of software principles. niel Kapl

How I reacted

- Almost all those tests are based on regression, so teach that.
- Techniques that give 1.5 digits of the p-value are good enough to start with.
- Students don't understand even simple formulas, so teach them the consequences of sampling by drawing actual samples.
- > Descriptive statistics should be rich: multiple regression and modeling, so that you can describe a complicated world.
- Teach basics of conditional probability so that p-values make sense.
- Create the worlds of the Null and Alternative hypothesis: draw data from them
- Variables are not lurking, they are there to be dealt with appropriately: measuring covariates, adjustment, randomization.

niel Kaplan

Teach Bonferroni, and worry about the details later.



A Religious Attitude

Proofiness

Emphasizing statements that are demonstrably **valid**, that is deducible from stated premises, but allowing the misconception/misinterpretation that the statements are therefore **true**, that is, applicable to the real world. Antonym: "truthiness."

Truthiness

Truthiness is a "truth" that a person claims to know intuitively "from the gut" without regard to evidence, logic, intellectual examination, or facts. Coined/popularized by Stephen Colbert in 2005.

Quotations Critiquing Proofiness

- "Far better an approximate answer to the right question, which is often vague, than an exact answer to the wrong question, which can always be made precise." — John Tukey
- ► "Essentially, all models are wrong, but some are useful." George E.P. Box
- "As far as the laws of mathematics refer to reality, they are not certain; as far as they are certain, they do not refer to reality." — Albert Einstein
- "Mathematicians do not study objects, but the relations between objects; to them it is a matter of indifference if these objects are replaced by others, provided that the relations do not change. Matter does not engage their attention, they are interested in form alone." — Henri Poincaré

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Proofiness: The Book



Charles Seife, *Proofiness: The Dark Arts of Mathematical Deception* "It all comes down to numbers, the author argues, and the ways they can be used to make people believe things that are not true." — David Pitt

I see this as a special form of Proofiness: the exploitation of people's willingness to believe arguments framed using numbers, since arithmetic is always **valid**, even if it's not always true. Synonym: **bullshit**.

Abstin

Bullshit

Philosopher Harry G. Frankfurt, in *On Bull-shit* (2005), writes about the bullshitter's complete disregard for whether what he's saying corresponds to facts in the physical world. He "does not reject the authority of the truth, as the liar does, and oppose himself to it. He pays no attention to it at all. By virtue of this, bullshit is a greater enemy of the truth than lies are."



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Two Different anti-Proofiness Attitudes

Approximation

Our answers are only rough. They need to be good enough to guide decisions. We also **need an operational way to see how rough our answers are** and whether they are good enough to guide our decisions.

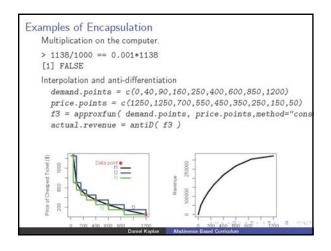
0.01 = 0.004769

0.10 = 0.50

Encapsulation/Information Hiding

Encapsulation is "the process of compartmentalizing the elements of an abstraction that constitute its structure and behavior; encapsulation serves to separate the contractual interface of an abstraction and its implementation." — Grady Booch

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An Example of Proofiness: The Alternative Hypothesis

A theoretical problem: Should the $\chi^2\text{-test}$ be one- or two-sided.

- Fisher: Two-sided. Too good a fit is a sign of a problem. "If P is between .1 and .9, there is no reason to suspect the hypothesis being tested." Fisher 1925, Statistical Methods for Research Workers, p. 71.
- Pearson: One-sided. We should not reject a "graduation curve" [a model of a distribution] because it is too close to the data.

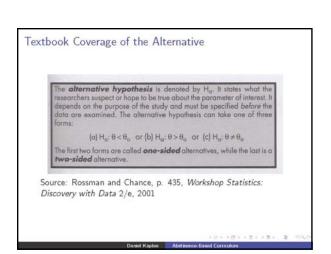
It's not clear to me who is right, since it depends on the **purpose** of the test. Looking for fraud, for signs of too many parameters, or flaws in the error model?

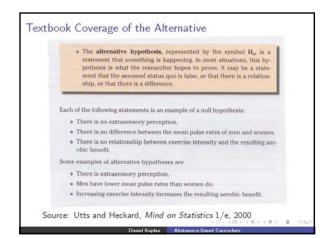
A theoretical resolution

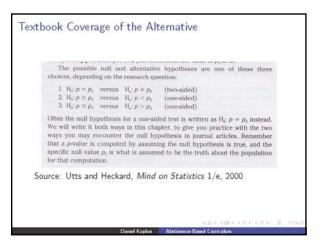
The Neyman-Pearson lemma. A one-tailed test gives greater power at any specified significance.

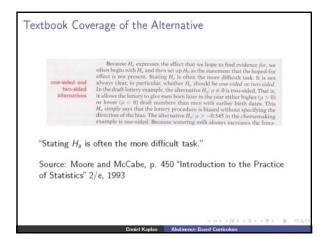
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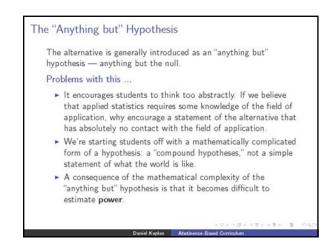
This doesn't really address the issue of the $\ensuremath{\textbf{purpose}}$ of the test, but ...











Costs and Benefits to One-Sided Tests

- Benefit: Increases the power (Neyman-Pearson Lemma) You can prove this!
- Cost (for teaching): Adds complexity.
- Cost (for teaching): Disconnects statistics from science. You don't have to talk about the specifics of the system when presenting examples.
- Cost (for teaching): Lost opportunity to teach about things that affect the results substantially, e.g., covariates and adjustment.
- Cost (for research): Encourages fraud ex post facto trimming of the p-value. Statistical circumcision. p < 0.10 is satisfactory, so long as you can justify a one-sided test.

How much does it increase the power? Is it worthwhile?

- Calculations indicate that for a study with 80% power, giving up the added power of the one-sided test is compensated by an approximately 20% increase in sample size.
- That's not nothing. But if we are going to be worrying about factors of 20% in sample size, we had better have already covered the matters that lead to order of magnitude estimates of sample size. This we typically have not done.
- Indeed, many statistics instructors that I talk to say that they don't cover power, and so how can a student understand the benefit of a one-sided test anyways?

Pedagogical Triage

It's a truism that our curricula are overwhelmed. There is too much to teach.

Triage

A process of determining the priority of patients treatments based on the severity of each patient's condition. Used when resources are insufficient for all patients to be treated immediately.



Triage in Statistics Education

First introduce the concept of hypothesis testing and give them the tools to get the first digit right, then worry about calculations on the order of 20%.

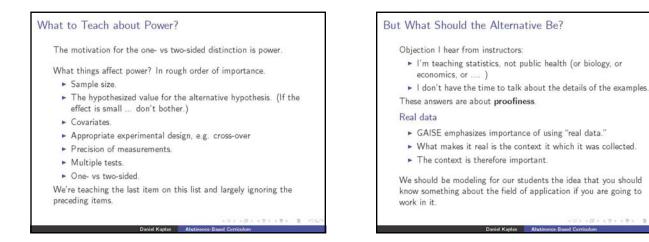
Proposal

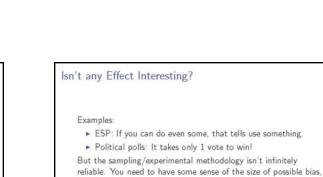
Make it a habit to develop every hypothesis testing example with a specific alternative hypothesis.

Not just the "direction" of the effect but the magnitude.

Benefits

- Helps to develop students' concepts of "significance" and how it differs from "substantial."
- Allows a discussion of sample size.
- Highlights the disconnect between the alternative and the p-value. ("But where did we use the alternative hypothesis?")
- Provides a connection to the practice of science. It's not usually the Null that you're interested in.





e.g., sampling of non-voters, cues to the ESP guesser. Austin Bradford Hill

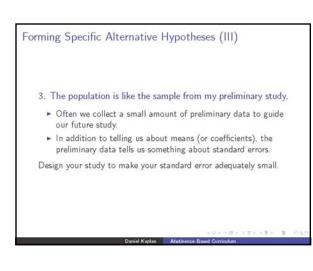
"The glitter of the t table diverts attention from the inadequacies of the fare."



Proofiness doesn't apply: you need to know about the world to frame a meaningful, specific alternative.

You need never be without a specific alternative.

- 1. Your best guess.
- 2. The smallest interesting effect.
- 3. The population is like your preliminary study.
- There's no such thing as the "right" alternative: it's a hypothesis!



A Proofiness Question

Suppose we have a single population that has been assigned **meaningless labels** randomly. We take a sample and measure some quantity. What can we say about how the labels relate to the measured quantity?

You can prove statements about this situation: the Null Hypothesis.

Label Type	Measurement type	Test
2 levels	quantitative	t-test
> 2 levels	quantitative	ANOVA
2 levels	2 levels	p-test
\geq 2 levels	\geq 2 levels	χ^2 test
quantitative	quantitative	F-test

But how does this relate to the real world?

A Worldly Dialog

Investigator: I think that trait A influences trait B. I recognize that there might be other traits — C, D, E, etc. — that could also be connected to A and B. How do I measure the extent to which A influences B?

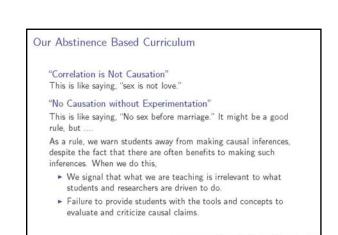
Statistician: Do an Experiment. Assign A in a way that's independent of C, D, E, etc. Then measure the association between A and B.

 ${\rm Investigator:}$ Nice! But, actually, I can't assign A. (Or, I can influence A, but C, D, E, will continue to play a role.) What do I do?

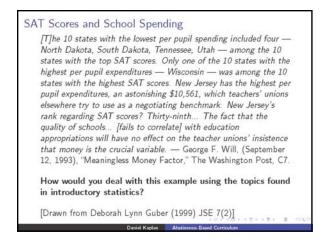
Statistician: Sorry. You're out of luck.

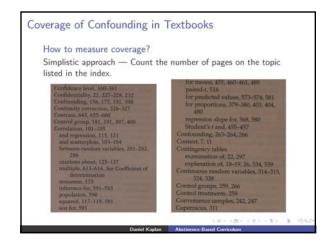
Overhearing the exchange, Econometrician/Political Scientist/Epidemiologist: May I help you?

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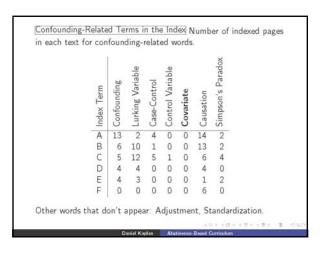


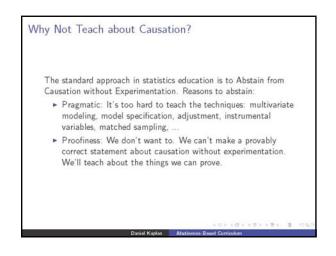
Books Surveyed

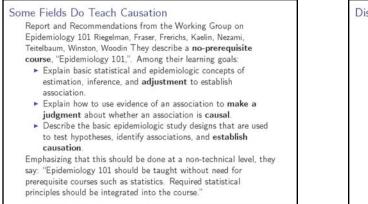
A Utts & Heckard, Mind on Statistics

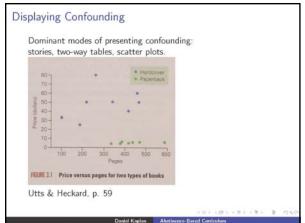
- B Moore & McCabe, Introduction to the Practice of Statistics 4/e
- C Agresti & Franklin, Statistics: The Art and Science of Learning from Data
- D Watkins, Scheaffer, & Cobb, Statistics in Action: Understanding a World of Data
- E De Veaux, Velleman, & Bock, Stats: Data and Models
- F McClave, Benson, & Sincich, Statistics for Business and Economics 9/e

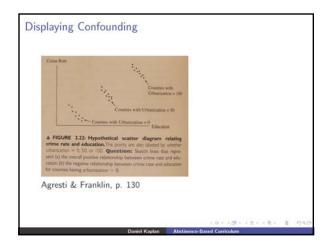
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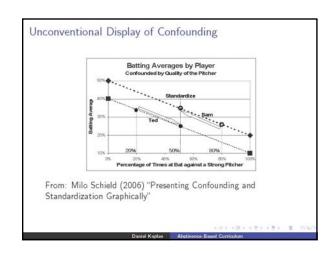


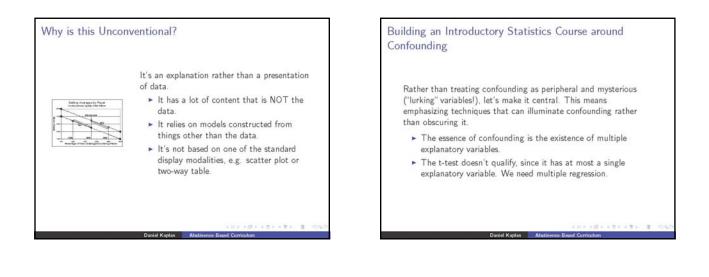


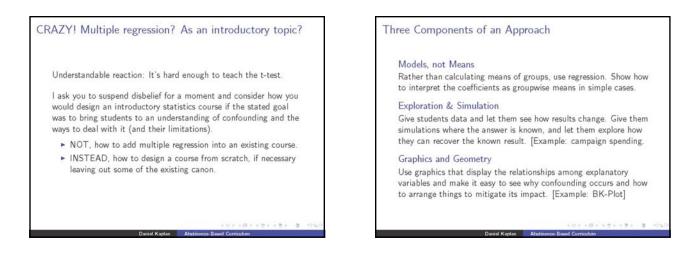


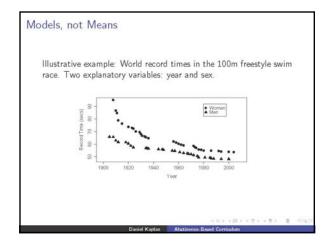


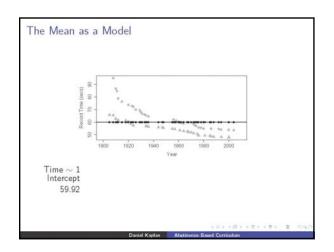
That is, let's skip the statistics education.

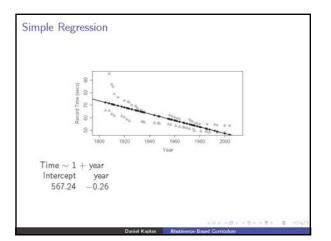


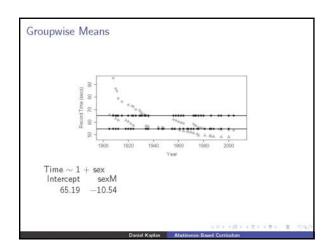


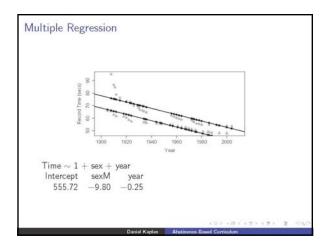


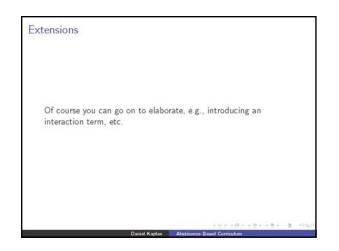












Summary

I believe that statistics has a huge amount to offer students across the curriculum. But statistics education...

- Has failed to embrace its natural allies: Computation and Approximation
- The dominance of proofiness
 - Pushes us to teach formal approaches to problems that are not of general interest.
 - Prevents us from prioritizing techniques. (Why do we spend time on one- and two-sided tests? Why teach equal and unequal variance tests?)

Let's use computation (encapsulation, packaging that makes daunting operations simple) and approximation (simulation, modeling) to allow us to teach meaningfully about causation.

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