Coincidence in Runs and Clusters

1

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Distribution of Longest Run of Successes

- N=2: Counts: 1, 2, 1: TT; HT, TH; HH N = 3: Counts: 1, 4, 2, 1. 0H: TTT. 1H: HTT, THT, TTH, HTH. 2H: HHT, THH. 3H: HHH.
- N = 10: 1, 143, 360, 269, 139, 64, 28, 12, 5, 2, 1. Mode=2, Median=3, Mean = 2.80.
- Mean <> 3, but close enough as a rule-of-thumb.

	Sumn Distributio	nary Stati	stics: gest Runs	;
K	N	Mode	Median	Mean
3	8	2	2	2.51
4	16	3	3	3.43
5	32	4	4	4.38
6	64	5	5	5.35
7	128	6	6	6.34
8	256	7	7	7.32
9	512	8	8	8.3
10	1,023	9	9	9.26





Conclusion

Students need to "see" that coincidences

- 1. are more common than expected
- 2. depend on the context
- 3. compare ex-ante with ex-post
- 4. may still be signs of causation (Cholera)
- That runs with 1 chance in N are generally found in N tries.



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		,	43				- (9			f _x	=R		DBE	TW	EEN	I(0,	9)
4	Α	В	С	D	Е	F	G	Н	1	J	K	L	Μ	Ν	0	Ρ	Q	R
3	9	3	2	9	9	4	1	9	9	9	2	2	5	3	5	0	5	5
4	8	0	6	4	1	6	7	4	0	2	2	0	3	7	0	9	8	0
5	3	1	7	3	5	2	5	6	8	7	2	0	4	8	9	2	9	6
6	9	0	1	4	3	4	2	8	9	2	6	6	4	7	7	9	2	3
7	9	6	2	1	9	0	4	3	8	6	2	7	5	7	5	1	3	3
8	4	3	6	1	5	8	1	9	4	8	4	9	2	6	1	8	7	2
9	0	0	2	4	3	0	5	5	9	3	1	6	9	5	3	5	8	4
10	9	6	6	7	5	0	6	6	1	2	6	6	0	9	3	6	7	8
11	9	1	0	4	7	4	2	4	4	0	4	3	8	8	4	9	8	5
12	9	8	0	1	4	6	0	8	2	0	4	2	3	5	6	4	5	7







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The "Birthday" Problem

- Q. What is the chance that two people in a group will have the same birth-date: month and day?
- A. One chance in 365?



18

20

The "Birthday" Problem

Richard von Mises (1883-1953) In a group of 28 people, a birthday match is "expected".

19

The "Birthday" Problem Math Answer

March 201

If the chance of an rare event is *p* and *p* =1/*k*, then this event is "expected" in k trials. In a group of size N, there are (N-1)(N/2) pairs. Solve for N(k). $k = (N-1)(N/2) = (N^2-N)/2$ Quadratic: $N^2 - N - 2k = 0$ Estimate: $\sim N^2/2 = 1/p$. Trial and error: $[27^2]/2 = 364 = 1/p = k$ Q. Are students convinced? No!!!

						March 2012				21	
		49	Co	nne	ctio	ons	: QI	uad	rant 1		
Schiel	d (201	1)	RICH	ARD V	ON MI	SES' E	BIRTH	DAY P	ROBLEM	28 P	eople
		Month	10	11	11	9	4	7	6		
		Day	16	18	8	9	13	25	24		
Month	Day									Month	Day
8	20							1		7	25
10	29									8	16
4	11									11	6
3	3									11	29
1	3									8	3
3	30									3	24
10	28									1	15
		Month	5	2	6	2	1	7	5		
		Dav	28	8	6	12	14	1	25		

						March 2012				22	
		49	Co	nne	ctio	ons	: Q	uad	rant 2	2	
Schiel	d (201	1)	RICH	ARD V	ON MI	SES' B	IRTH	DAY P	ROBLEM	28 P	eop
		Month	8	12	7	11	6	4	2		
		Day	28	2	15	15	5	24	2		
Month	Day									Month	Da
10	8									2	5
5	17									2	17
9	13									12	26
11	18									3	6
12	21		1					2		4	20
2	28									10	2
10	11									3	23
		Month	10	7	4	12	8	4	8		
		Dav	22	22	10	6	4	20	21		



						March 2012				24	
		49	Co	nne	ctic	ons	: QI	uad	rant 4	L.	
Schield	1 (201	1)	RICH	ARD V	ON MI	SES' E	BIRTH	DAY P	ROBLEM	28 P	eop
		Month	11	11	3	5	1	5	2		
		Day	5	27	17	3	5	19	4		
Month	Day	- Superio								Month	Da
11	5		4							11	12
11	17									8	24
8	2									5	1
4	26									3	28
4	22									10	13
10	8									4	4
12	22									8	11
		Month	1	7	5	5	12	10	5		
		Dav	2	1	23	7	20	14	14		













	March 2012							
Connections and Chance								
Pairs	GROUP	Details						
196	Quadrants 1-4	49 pairs each						
49	Side-to-Side							
49	Top-to-Bottom							
84	Within each side	21 pairs each						
378	TOTAL							
A "birthday" m	natch has one chance	in 365.						
n a group of 2	8, we have 378 pairs:	: (N-1)(N/2).						
A match is exp	ected: Match is more	likely than not.						



ASA Chapter & StatChat May 9 Wednesday 6 PM Augsburg

Wed May 9. Augsburg College. 6-9 PM. Supper Chapter website: <u>www.amstat.org/chapters/twincities/</u>

SPEAKERS:

Marc Isaacson: Teaching Activities

Robert Raymond: Untangling a Conundrum.

Milo Schield: Introducing the Matrixx Case

Danny Kaplan: Comments on US Supreme Court Matrixx Case: Is Significance Significant?