| Reading |
| :---: |
| Graphs and Trables |
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## Scatter Plot: Association/Causation

5a: Adults who weigh more tend to be taller than those who weigh less? YES: Student error rate: $25 \%$

5b: If an adult increases their weight, they can expect to increase their height? NO: 19\%


## Reading <br> Tables and Graphs

- Easy when data involves counts or totals.
- Harder with rates. E.g., birth/death rates.
- Difficult with percentages.

Why?
Confusion of the inverse. $\mathrm{P}(\mathrm{A} \mid \mathrm{B}) \neq \mathrm{P}(\mathrm{B} \mid \mathrm{A})$.

- Irrelevant with counts or totals
- Unlikely with low rates: 3 moms/100 babies
- Common when dealing with percentages.


## Scatter Plot: the Ecological Fallacy

6a: As the percentage of Protestants increases, the suicide rate tends to increase. YES: $34 \%$ wrong 6b: Protestants are more likely to commit suicide than non-Protestants (are). NO: 45\% wrong
Saying "Yes" to 6 b involves the ‘ecological fallacy': going from groups to sub-groups.

| 100\% Row Table: Descriptions |  |  |  |
| :---: | :---: | :---: | :---: |
| 7a: $25 \%$ of females are blacks? NO: $44 \%$ wrong <br> $7 \mathrm{~b}: 25 \%$ is the percentage of blacks among females? <br> NO: 38\% wrong |  |  |  |
|  | SEX |  |  |
| RACE | Male | Female | TOTAL |
| Black | 75\% | 25\% | 100\% |
| White | 50\% | 50\% | 100\% |
| Other | 40\% | 60\% | 100\% |
| TOTAL | 50\% | 50\% | 100\% |

## 100\% Row Table: Comparisons

8a: Females are two times as likely to be white as to be black? NO: 44\%
8b: Whites are two times as likely to be female than are blacks NO: 60\%

8c: Whites are two times more likely to be female than are blacks? NO: 65\%

|  | SEX |  |  |
| :---: | :---: | :---: | :---: |
| RACE | Male | Female | TOTAL |
| Black | $75 \%$ | $25 \%$ | $100 \%$ |
| White | $50 \%$ | $\mathbf{5 0 \%}$ | $100 \%$ |
| Other | $40 \%$ | $60 \%$ | $100 \%$ |
| TOTAL | $50 \%$ | $50 \%$ | $100 \%$ |


| Two-Way Half Tables: Descriptions |  |  |  |
| :---: | :---: | :---: | :---: |
| 9a: $20 \%$ of runners are female smokers? NO: $55 \%$ <br> 9b: $20 \%$ of females are runners who smoke? NO: $53 \%$ <br> 9c: $20 \%$ of female smokers are runners? YES: $62 \%$ <br> 9d: $20 \%$ of smokers are females who run? NO: $42 \%$ |  |  |  |
| PERCENTAGE WHO ARE RUNNERS |  |  |  |
|  | Non-smoker | Smoker | Total |
| Female | 50\% | 20\% | 40\% |
| Male | 25\% | 10\% | 20\% |
| Total | 37\% | 15\% | 30\% |

## Two-Way Half Tables: Comparisons

10a: The percentage of smokers who run is twice as much among females as among males? YES: 42\%
10b. The percentage of runners is twice as much among female smokers as among male smokers? YES: 41\%

| PERCENTAGE WHO ARE RUNNERS |  |  |  |
| :---: | :---: | :---: | :---: |
|  | Non-smoker | Smoker | Total |
| Female | $50 \%$ | $20 \%$ | $40 \%$ |
| Male | $25 \%$ | $\mathbf{1 0} \%$ | $20 \%$ |
| Total | $37 \%$ | $15 \%$ | $30 \%$ |

## Simpson's Paradox

A research hospital had a higher death rate than a rural hospital. Each patient's condition was classified as either "poor" or "fair."
Q11. Is it possible that this research hospital had a lower death rate than this rural hospital for those patients in "poor" condition AND for those patients in "fair" condition?
Choice of answers: Yes, No, Don't know.
YES: College student error rate: 44\%

## Multiple Half-Tables: Description

Assume, "In 1990" ahead of each statement:
12a: $26.2 \%$ of blacks were smokers. YES: $60 \%$
12b: $26.2 \%$ of smokers were black NO: $72 \%$

| Table 3: Percentage of Smoking Prevalence |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Year | All | Male | Female | White | Black |  |
| 1955 | -- | 56.9 | 28.4 |  | -- | -- |
| 1965 | 42.4 | 51.9 | 33.9 |  | 42.1 | 45.8 |
| 1980 | 33.2 | 37.6 | 29.3 |  | 32.9 | 36.9 |
| 1990 | 25.5 | 28.4 | 22.8 |  | 25.6 | 26.2 |


| Multiple Falf-Tables: Description |  |  |  |
| :---: | :---: | :---: | :---: |
| Assume, "In US in 1996" ahead of each statement: 13a: $6 \%$ of low-weight births were in Calif. NO: $60 \%$ 13b: $6 \%$ of Calif. births were low-weight. YES: $39 \%$ |  |  |  |
| Percent of Births with Low Birth Weight |  |  |  |
| State | 1990 | 1995 | 1996 |
| U.S. | 7 | 7.3 | 7.4 |
| Alabama (AL) | 8.4 | 9 | 9.3 |
| California (CA) | 5.8 | 6.1 | 6 ) |

## Multiple Half-Tables: Description

Assume, "In US in 1996" ahead of each statement: 13a: $6 \%$ of low-weight births were in Calif. NO: 60\% 13b: $6 \%$ of Calif. births were low-weight. YES: $39 \%$

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Multiple Half-Tables: Description

Q15a. 10\% of these women who received an HIV test were ages 40 to 44 ? NO: $78 \%$

Table 5: Percent of Women, 15 to 44, who Received Selected Medical Services

Q15b. 10\% of these women ages 40 to 44 had an HIV test? YES: 66\%

| Age | HIV | Pregnancy | Pap |
| :---: | :---: | :---: | :---: |
| $15-19$ | 14.6 | 16.1 | 33.5 |
| $20-24$ | 20 | 27.4 | 68.7 |
| $25-29$ | 25.6 | 25.3 | 70.9 |
| $30-34$ | 18.5 | 17.4 | 69.5 |
| $35-39$ | 14.2 | 8.1 | 62.9 |
| $40-44$ | 10 | 4.3 | 62.7 |
| ALL | 17.3 | 16 | 61.9 |

92\% of respondents agreed that
"College students should be able to read these tables and graphs."
$90 \%$ of respondents agreed that
"These tables and graphs are the kind I need or want to be able to read or understand."
$75 \%$ of respondents agreed that
"This survey was much more difficult than I thought it would be."

## Multiple Half-Tables: Comparison

14. In the US in 1996, there were more low-weight births in Alabama (AL) than in California (CA).
NO. No named ratio keyword. Student error rate: 66\%

| Percent of Births with Low Birth Weight |  |  |  |
| :--- | :---: | :---: | :---: |
| State | $\mathbf{1 9 9 0}$ | $\mathbf{1 9 9 5}$ | $\mathbf{1 9 9 6}$ |
| U.S. | 7 | 7.3 | 7.4 |
|  |  |  |  |
| Alabama (AL) | 8.4 | 9 | 9.3 |
| California (CA) | 5.8 | 6.1 | 6 |


| Multiple Falforables: <br> Comparison <br> Q16a: Women 40-44 were twice as likely to have an HIV test as were women 20-24? YES 32\% |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |
| Q16b: <br> Women 20-24 were two times more likely to have an HIV test than were women 40-44? <br> NO 82\% | Percent of Women, 15 to 44, who Received Selected Medical Services |  |  |  |
|  | Age | HIV | Pregnancy | Pap |
|  | 15-19 | 14.6 | 16.1 | 33.5 |
|  | 20-24 | 20 | 27.4 | 68.7 |
|  | 25-29 | 25.6 | 25.3 | 70.9 |
|  | 30-34 | 18.5 | 17.4 | 69.5 |
|  | 35-39 | 14.2 | 8.1 | 62.9 |
|  | 40-44 | 10 | 4.3 | 62.7 |
|  | ALL | 17.3 | 16 | 61.9 |

## Multiple Half-Tables:

 ComparisonQ16a: Women 40-44 were twice as likely to have an HIV test as were women 20-24? YES 32\%

Q16b:
Women 20-24
were two times more likely to have an HIV test than were women
40-44? NO 82\%

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AL-16.3

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## StatLit Survey Eyror Rate

The average error rate was about

- $50 \%$ for college students,
- $45 \%$ for data analysts and
- $30 \%$ for college teachers.

Using data analysts’ 80th percentile score (67\% correct), the following reached that level:

- $5 \%$ of students,
- $20 \%$ of data analysts
- $45 \%$ of college teachers

> | Conclusion |
| :--- |
| Describing and comparing rates \& percentages is |
| conditional probability in ordinary English. |
| Statistical educators will be seen as negligent |
| if most of their students cannot read - much less |
|  |
| percentages as presented in tables and graphs. |
| Statistical educators should accept responsibility for |
| teaching students how to read and write ordinary |
| English descriptions and comparisons of rates and |
| percentages as found in tables and graphs. |

## Recommendations

Try out the simple 5-table survey on your students: www.StatLit.org/Survey. Paper copy available.

Try out the on-line grammar checker program. www.StatLit.org/RSVP.
Give your students a table or graph involving rates or percentages. Have them describe a single ratio (or compare two ratios) using ordinary English.
Try teaching this in your intro stats class.

| Related Articless at |
| :--- |
| WWW. StatLit.Org |
| Whield, Milo (2004). Statistical Literacy and Liberal Education at |
| Augsburg College. AAC\&U Peer Review. See |
| www.StatLit.org/pdf/2004SchieldAACU.pdf. |
| Schield, Milo (2000). Difficulties in Describing and Comparing |
| Rates and Percentages. 2000 ASA Section on Statistical Education. |
| P. 176. See www.StatLit.org/pdf/2000SchieldASA.pdf. |
| Schield, Milo (2001). Statistical Literacy: Reading Tables of Rates |
| and Percentage. ASA Proceedings of Statistical Education Section. |
| See www.StatLit.org/pdf/2001SchieldASA.pdf |
| Schield, Milo (2004). Statistical Literacy Curriculum Design. |
| IASE. See www.StatLit.org/pdf/2004SchieldIASE.pdf. |

## Survey Subjects Comfort with Stats

"Very comfortable" dealing with formal statistics: sampling distributions, confidence intervals.

- $0 \%$ of students,
- $30 \%$ of data analysts and
- $57 \%$ of college professors.
"Very comfortable" dealing with informal statistics: rates and percentages in tables and graphs
- $7 \%$ of students,
- $62 \%$ of data analysts and
- $76 \%$ of college professors.

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