Log-Normal Distribution of Households by Income

А	В	С	D	E	F	G	Н	I	Row
	Real-wo	rld statisti	cs		mu	3.912	=LN(B4)		2
	Manual I	entry			mu+S^2/2	4.382	=LN(B5)		3
median	50				Sigma^2	0.940	=2*(G3-G2)		4
mean	80				Sigma	0.970	=SQRT(G4)		5
Underlying math statistics									6
B9	B9 = Exp(G2-G4)								7
	Mode	PDF	C9						8
	19.531 1.32E-02 =LOGNORM.DIST(B9,G\$2,G\$5,0)								9
А	В	С	D	E	F	G	Н	I	10
	B14	C14	D14	E14	C14				11
=/	A14*B\$4	Copy F12	=C14/C\$9	Copy F14	=LOGNOR	M.DIST(B14,\$G\$2,\$G	\$5,0)	12
Scale	Income	PDF	% of mode	CDF	E14				13
0.1	5	4.90E-03	37.2%	0.9%	=LOGNOR	M.DIST(B14,G\$2,G\$5	,1)	14
0.2	10	1.04E-02	78.8%	4.8%					15
0.3	15	1.27E-02	96.4%	10.7%	Table:	Distribu	tion of subjee	cts	16
0.4	20	1.32E-02	100.0%	17.2%			by income (\$	\$1,000)	17
0.5	25	1.27E-02	96.8%	23.7%					18
0.7	35	1.10E-02	83.4%	35.6%	PDF: P	robability	Density Fund	tion	19
1	50	8.23E-03	62.5%	50.0%					20
1.6	80	4.57E-03	34.7%	68.6%	CDF: C	umulative	e Distribution F	Function	21
2	100	3.19E-03	24.2%	76.3%	CDF: Pe	ercentage	e of subjects v	vho	22
3	150	1.44E-03	11.0%	87.1%		have inc	ome below Co	ol B.	23
4	200	7.40E-04	5.6%	92.4%					24
5	250	4.15E-04	3.2%	95.2%					25
6	300	2.49E-04	1.9%	96.8%					26
8	400	1.03E-04	0.8%	98.4%					27
10	500	4.90E-05	0.4%	99.1%	l				28



DEFINITIONS OF COLUMNS IN TABLE (subjects organized by amount)

- B13 X Income (\$1,000)
- C13 PDF Probability density function: Not the percentage of subjects who have income X
- D13 **PDF as % of modal PDF:** Pctg. who have income X as % of those who have modal income
- E13 **CDF** Cumulative density function: **Percentage of subjects who have incomes BELOW X** Note1: "*Subjects*" is the whole; "*incomes below X*" is the part. Note2: B20 always equals the median amount Note3: E20 (the percentage of subjects having incomes below the median) is always 50%.
- Cell E22: 76.3% of subjects have incomes below (less than) \$100,000.

PRACTICE QUESTIONS: Assume subjects are distributed log-normally by amount.

The answers to all these questions are found in the table -- not in the graph. All questions involve just columns B and E: Income and cumulative percentage of subjects

Set median = \$50K; Set mean = \$80K

- 4.8%
- a Q. What percentage of subjects have incomes BELOW 10K? Solution: Find 10K in Column B are row 15. Find CDF in same row, column E,
- 95.2%

Q. What percentage of subjects have incomes ABOVE 10K?
Solution: Subtract 4.8% from 100% to get 95.2%. Note: "Above" plus "Below" = 100%

Set median = \$50K; Set mean = \$75K

67.4%

- c Q. What percentage of subjects have incomes BELOW 75K? Solution: Enter 75 into B5. Find 75K in column B, row 21. Find CDF in row 21.
- 32.6% d Q. What percentage of subjects have incomes ABOVE 75K? Solution: Subtract 67.4% from 100% to get 32.6%. Note: "Above" + "Below" = 100%.