

**Hypothesis Tests using
Excel Z.TEST Function**

by
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*Slides and audio at: [www.StatLit.org/
pdf/ZTEST-Function-Excel-2008-6up.pdf](http://www.StatLit.org/pdf/ZTEST-Function-Excel-2008-6up.pdf)
[Audio/ZTEST-Function-Excel-2008.mp3](http://www.StatLit.org/audi/ZTEST-Function-Excel-2008.mp3)*

Function: ZTEST

Purpose: Calculate the likelihood of getting the sample statistic (or more extreme) by chance – assuming null hypothesis is true.

FEATURES:

Assumptions: There is a single population
Population standard deviation is known.

Nature: Excel functions automatically updated if data changes.

Three Arguments (or Inputs):

- 1) Range or Array: the range of sample data being tested
- 2) Mu-zero: Value of the null hypothesis
- 3) Sigma: Standard deviation of population

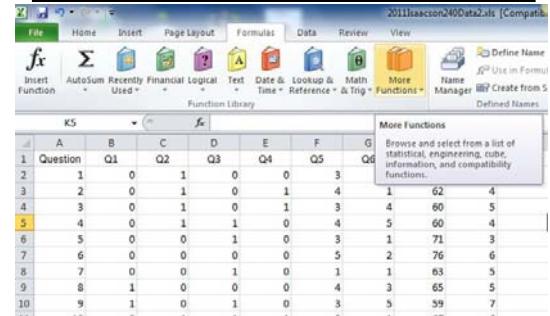
**Run Hypothesis Tests
from this data: B1:I241**

Data for Q1-Q4 (B-E) is Binary: 0=No, 1=Yes.
Data for Q5-Q6 (F-G) is Ordinal (discrete): 1-5.
Data for Q7-Q8 (H-I) is Quantitative (ratio).

| | A | B | C | D | E | F | G | H | I |
|---|----|----|----|----|----|----|----|----|----|
| 1 | ID | Q1 | Q2 | Q3 | Q4 | Q5 | Q6 | Q7 | Q8 |
| 2 | 1 | 0 | 1 | 0 | 0 | 3 | 5 | 67 | 5 |
| 3 | 2 | 0 | 1 | 0 | 1 | 4 | 1 | 62 | 4 |
| 4 | 3 | 0 | 1 | 0 | 1 | 3 | 4 | 60 | 5 |
| 5 | 4 | 0 | 1 | 1 | 0 | 4 | 5 | 60 | 4 |
| 6 | 5 | 0 | 0 | 1 | 0 | 3 | 1 | 71 | 3 |

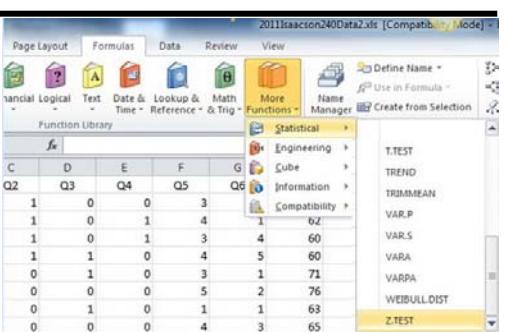
Excel instructions and data at:
www.StatLit.org/xls/2012Isaacson240Data.xls

**A: From the Formula ribbon,
Select “More Functions”**



The screenshot shows the Microsoft Excel 2008 ribbon with the 'Formulas' tab selected. Below the ribbon, a dropdown menu titled 'Function Library' is open, showing a grid of function names. The 'More Functions' option is highlighted in yellow.

**B: Select ‘Statistical’
and then select ‘Z.Test’**



The screenshot shows the Microsoft Excel 2008 ribbon with the 'Formulas' tab selected. Below the ribbon, a dropdown menu titled 'Function Library' is open, showing the 'Statistical' category. The 'Z.TEST' function is highlighted in yellow.

GOAL

How to conduct a one-population hypothesis-test using the Excel 2008 Z.TEST function in two situations:

- 1) Test of Measurements
- 2) Test of Proportions

Assumption: Population standard deviation is known.

Notation for the three arguments of Z.TEST function:

- Array: the range of the sample data.
- X: The value, mu, of the null hypothesis.
- Sigma: The population standard deviation.

**1a Z.Test for Measures:
Sigma is known (entered)**

The dialog box shows the following settings:

- Array: H1:H4
- X: 62
- Sigma: 3.605551

Formula result = 0.315477008

Sample mean is 63
P-value is 0.315...

**1b Z.Test for Measures:
Sigma is estimated from sample**

The dialog box shows the following settings:

- Leave blank
- Array: H1:H4
- X: 62
- Sigma: (Leave blank)

Formula result = 0.315477021

Sample standard deviation is 3.605551
Note: the p-value is still 0.315 (with n=3)

**1c Z.Test for Measures:
Summary**

The sample standard deviation can be used to estimate the population standard deviation.

There is no adjustment for this new source of variation. This modified Z.TEST is not the same as a T-TEST.

Using the sample standard deviation for small samples ($n < 30$) can result in p-values that smaller than those given by a T-Test. This increases false positives.

**2a: Test for Proportions
Sigma is entered**

The dialog box shows the following settings:

- Array: C1:C241
- X: 0.25
- Sigma: 0.44953

Formula result = 0.15740719

This analysis assumes the data are zeros and ones.
In this case, the mean is always the proportions of ones.
Sample mean is 0.28
P-value is 0.1574...

**2b: Test for Proportions
Sigma is estimated from sample**

The dialog box shows the following settings:

- Leave blank
- Array: C1:C241
- X: 0.25
- Sigma: (Leave blank)

Formula result = 0.15740916

Sample mean (p) is 0.28. $p^*q = 0.2016$
Sample Std Dev = $\text{Sqrt}(p^*q) = \text{Sqrt}(0.2016) = .4495$
P-value is 0.1574....

Conclusions

Excel 2008 offers a single-population Z-Test function for measures and proportions. It does not offer a single-population T-Test.

To use this function for proportions, the outcomes must be coded as zero and one.

Excel can do this test when the proportions are coded differently from zero and one. Showing how is beyond the scope of this presentation.

Excel does allow for two-tail tests, but that is more involved. See the Excel Help system for details.

B: From “More Functions”, select “Statistical”

The screenshot shows the 'More Functions' dialog box in Excel 2008. The 'Statistical' category is open, and the 'Z.TEST' function is highlighted with a yellow box. The data range A1:F11 is selected in the formula bar.

C: From “Statistical”, select “Z.Test”

The screenshot shows the 'Statistical' category in the Function Library of Excel 2008. The 'Z.TEST' function is highlighted with a yellow box.

2c Z.Test for Proportions: Summary

Z.TEST is a good hypothesis test of proportions in a single population if the data is coded as zero and one.

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| 6 | 5 | 0 | 0 | 1 | 0 | 3 | 1 | 71 | 3 |

Excel instructions and data at:

www.StatLit.org/xls/2012Isaacson240Data.xls

A: From the Formula ribbon, Select “More Functions”

The screenshot shows a Microsoft Excel 2008 window with the title bar "2011Isaacson240Data2.xls [Compatibility Mode]". The ribbon is visible with tabs: File, Home, Insert, Page Layout, Formulas (selected), Data, Review, and View. In the Formulas tab, the "Function Library" group is open, showing icons for AutoSum, Recently Used, Financial, Logical, Text, Date & Time, Lookup & Reference, Math & Trig, and More Functions. The "More Functions" icon is highlighted with a yellow background. A tooltip for "More Functions" is displayed, stating: "Browse and select from a list of statistical, engineering, cube, information, and compatibility functions." The main worksheet area shows a data table with columns labeled A through G and rows numbered 1 through 11. Column A contains labels "Question", "Q1", "Q2", "Q3", "Q4", "Q5", and "Q6". The data values range from 0 to 10.

| | A | B | C | D | E | F | G |
|----|----------|----|----|----|----|----|----|
| 1 | Question | Q1 | Q2 | Q3 | Q4 | Q5 | Q6 |
| 2 | 1 | 0 | 1 | 0 | 0 | 3 | |
| 3 | 2 | 0 | 1 | 0 | 1 | 4 | |
| 4 | 3 | 0 | 1 | 0 | 1 | 3 | |
| 5 | 4 | 0 | 1 | 1 | 0 | 4 | |
| 6 | 5 | 0 | 0 | 1 | 0 | 3 | |
| 7 | 6 | 0 | 0 | 0 | 0 | 5 | |
| 8 | 7 | 0 | 0 | 1 | 0 | 1 | |
| 9 | 8 | 1 | 0 | 0 | 0 | 4 | |
| 10 | 9 | 1 | 0 | 1 | 0 | 3 | |
| 11 | 10 | 0 | 1 | 1 | 1 | 2 | |

B: Select 'Statistical' and then select 'Z.Test'

The screenshot shows the Microsoft Excel 2008 ribbon at the top with tabs: Page Layout, Formulas, Data, Review, and View. The 'Formulas' tab is selected. Below the ribbon is the 'Function Library' group, which includes categories: Financial, Logical, Text, Date & Time, Lookup & Reference, Math & Trig, and More Functions. The 'More Functions' button is highlighted. A dropdown menu is open under 'More Functions', showing categories: Statistical, Engineering, Cube, Information, and Compatibility. The 'Statistical' category is also highlighted. To the right of the dropdown, a list of statistical functions is displayed, with 'Z.TEST' highlighted in yellow. The main workspace shows a data table with columns labeled Q2 through Q6 and rows labeled 1 through 8.

| C | D | E | F | G |
|----|----|----|----|----|
| Q2 | Q3 | Q4 | Q5 | Q6 |
| 1 | 0 | 0 | 3 | |
| 1 | 0 | 1 | 4 | |
| 1 | 0 | 1 | 3 | |
| 1 | 1 | 0 | 4 | |
| 0 | 1 | 0 | 3 | |
| 0 | 0 | 0 | 5 | |
| 0 | 1 | 0 | 1 | |
| 0 | 0 | 0 | 4 | |

T.TEST
TREND
TRIMMEAN
VAR.P
VAR.S
VARA
VARPA
WEIBULL.DIST
Z.TEST

GOAL

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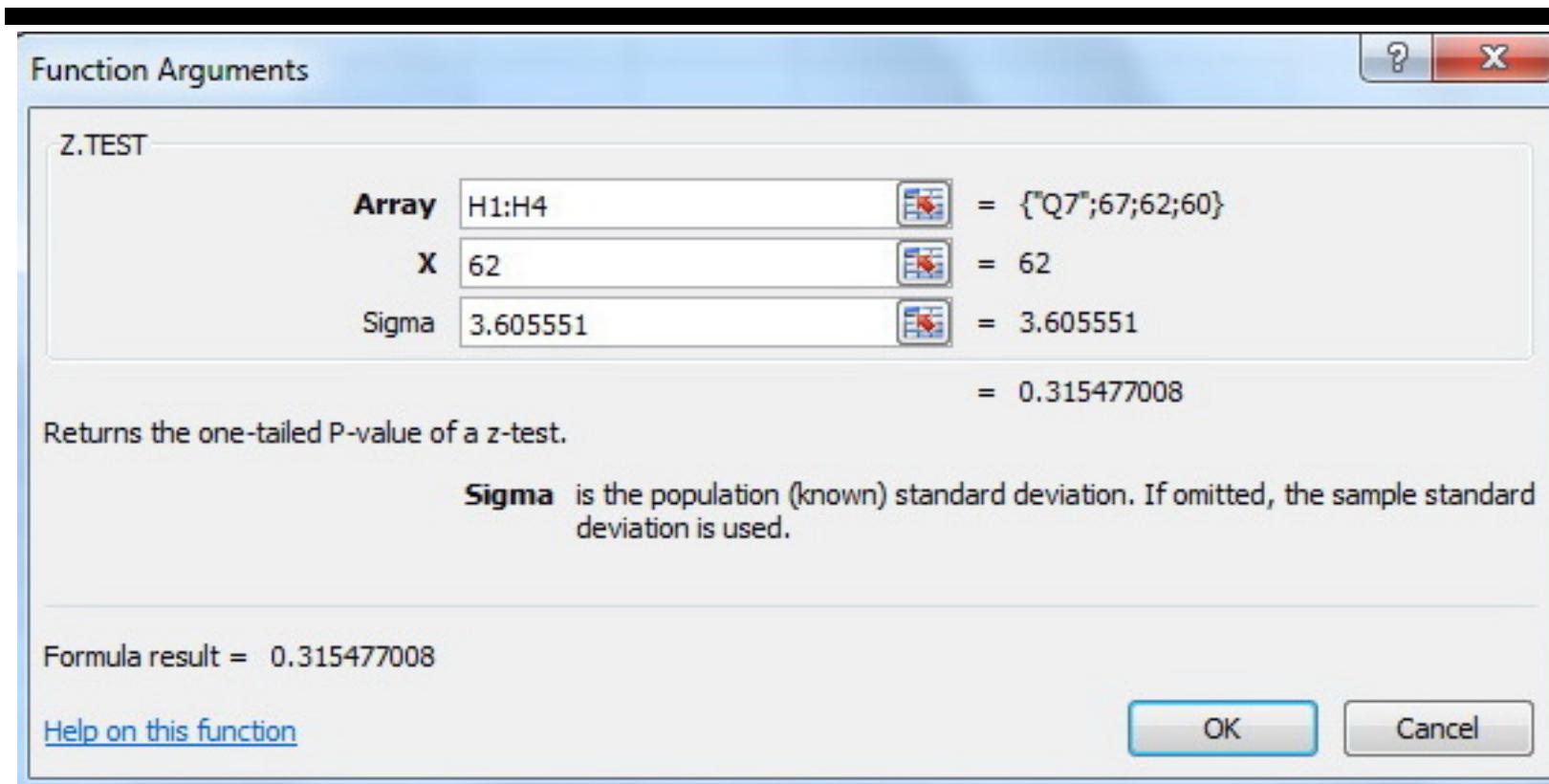
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- 2) Test of Proportions

Assumption: Population standard deviation is known.

Notation for the three arguments of Z.TEST function:

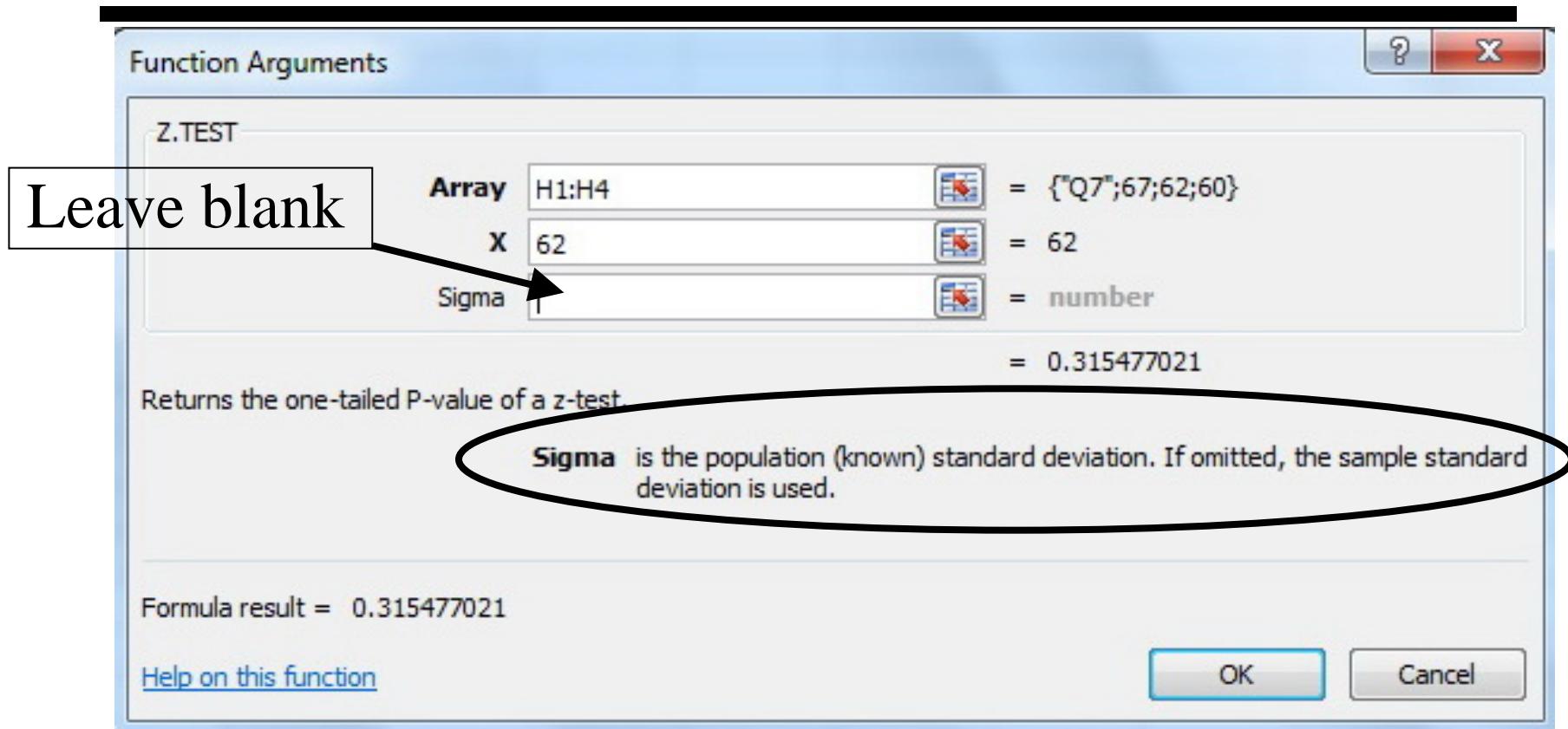
- Array: the range of the sample data.
- X: The value, mu, of the null hypothesis.
- Sigma: The population standard deviation.

1a Z.Test for Measures: Sigma is known (entered)



Sample mean is 63
P-value is 0.315...

1b Z.Test for Measures: Sigma is estimated from sample



Sample standard deviation is 3.605551
Note: the p-value is still 0.315 (with n=3)

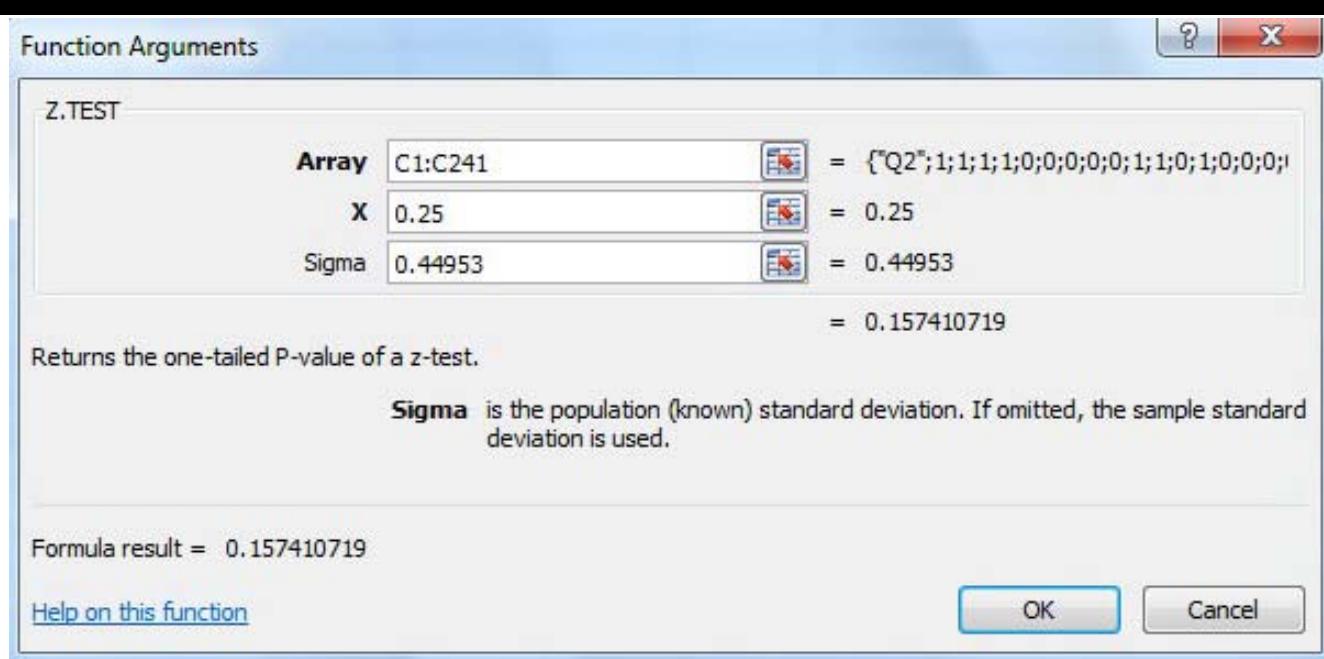
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There is no adjustment for this new source of variation. This modified Z.TEST is not the same as a T-TEST.

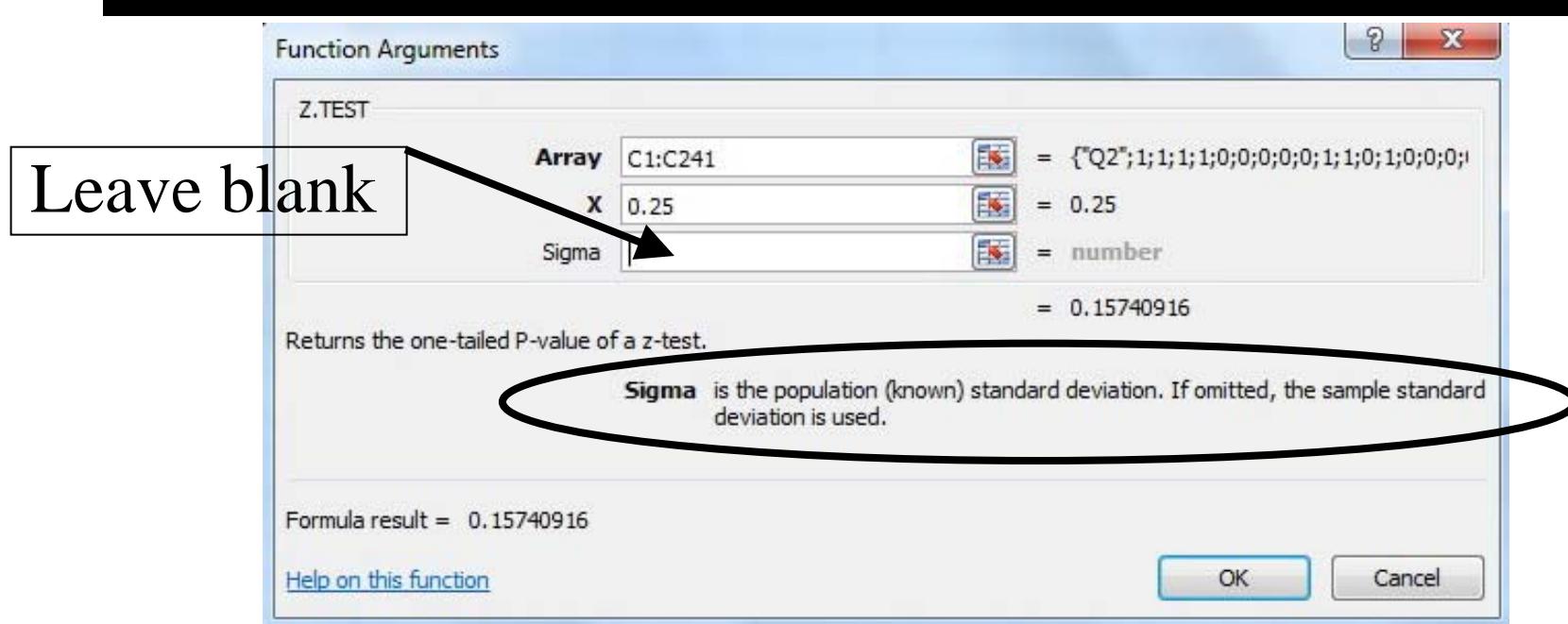
Using the sample standard deviation for small samples ($n < 30$) can result in p-values that smaller than those given by a T-Test. This increases false positives.

2a: Test for Proportions Sigma is entered



This analysis assumes the data are zeros and ones.
In this case, the mean is always the proportions of ones.
Sample mean is 0.28
P-value is 0.1574...

2b: Test for Proportions Sigma is estimated from sample



Sample mean (p) is 0.28. $p^*q = 0.2016$
Sample Std Dev = $\text{Sqrt}(p^*q) = \text{Sqrt}(0.2016) = .4495$
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Excel does allow for two-tail tests, but that is more involved. See the Excel Help system for details.

B: From “More Functions”, select “Statistical”

The screenshot shows a Microsoft Excel 2008 window with the ribbon menu at the top. The 'Formulas' tab is selected. In the 'Function Library' group, the 'More Functions' button is highlighted. A dropdown menu is open, showing categories: 'Statistical' (which is also highlighted), 'Engineering', 'Cube', 'Information', and 'Compatibility'. Below the categories, there are two more items: '101' and '62'. The main worksheet area displays a table with columns labeled 'A' through 'G' and rows numbered 1 to 11. The data in the table represents survey results for six questions (Q1-Q6) across 11 respondents.

| | A | B | C | D | E | F | G |
|----|----------|----|----|----|----|----|----|
| 1 | Question | Q1 | Q2 | Q3 | Q4 | Q5 | Q6 |
| 2 | 1 | 0 | 1 | 0 | 0 | 3 | |
| 3 | 2 | 0 | 1 | 0 | 1 | 4 | |
| 4 | 3 | 0 | 1 | 0 | 1 | 3 | |
| 5 | 4 | 0 | 1 | 1 | 0 | 4 | |
| 6 | 5 | 0 | 0 | 1 | 0 | 3 | |
| 7 | 6 | 0 | 0 | 0 | 0 | 5 | |
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| 9 | 8 | 1 | 0 | 0 | 0 | 4 | |
| 10 | 9 | 1 | 0 | 1 | 0 | 3 | |
| 11 | 10 | 0 | 1 | 1 | 1 | 2 | |

C: From “Statistical”, select “Z.Test”

The screenshot shows the Microsoft Excel 2011 ribbon at the top. The 'Formulas' tab is selected. Below it, the 'Function Library' is open, showing categories: Financial, Logical, Text, Date & Time, Lookup & Reference, and Math & Trig. A dropdown menu from the 'More Functions' category is open, listing Statistical, Engineering, Cube, Information, and Compatibility. Under the Compatibility category, the 'Z.TEST' function is highlighted. The main area of the screen shows a portion of a worksheet with columns C through G and rows Q2 through Q10.

| C | D | E | F | G |
|----|----|----|----|----|
| Q2 | Q3 | Q4 | Q5 | Q6 |
| 1 | 0 | 0 | 3 | |
| 1 | 0 | 1 | 4 | |
| 1 | 0 | 1 | 3 | |
| 1 | 1 | 0 | 4 | |
| 0 | 1 | 0 | 3 | |
| 0 | 0 | 0 | 5 | |
| 0 | 1 | 0 | 1 | |
| 0 | 0 | 0 | 4 | |

2c Z.Test for Proportions: Summary

Z.TEST is a good hypothesis test of proportions in a single population if the data is coded as zero and one.